Charged Higgs Production via Bottom Partons

Tilman Plehn, CERN

- MSSM Higgs Bosons at the LHC
- Bottom Parton Description
- Charged Higgs Production at NLO
- SUSY-QCD Corrections

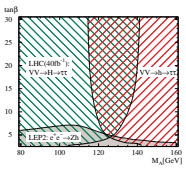
MSSM Higgs Bosons at the LHC

MSSM Higgs Sector

- two doublets, coupling to up and down type fermions
  → five physical states $h^o, H^o, A^o, H^\pm$
  → mixing of scalars to mass eigenstates (mixing angle α)
  → more predictive than Standard Model (upper h^o mass limit)
- conveniently expressed as function of m_A and $\tan\beta \equiv v_2/v_1$
- Yukawa couplings: $(m_b \tan\beta, m_t/\tan\beta)$

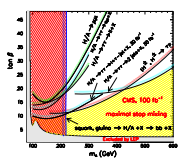
LHC search channels

- multitude of channels [ATLAS TDR (pre-LEP2)]
- complete coverage by WBF $h \to \tau\tau$ [TP, Rainwater, Zeppenfeld]
- mostly light scalar Higgs boson

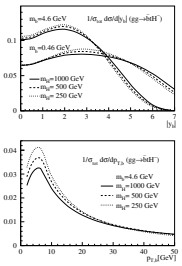


Tell it is 2HDM (MSSM?) ⇒ look for heavy Higgs bosons

- $H^0, A^0 \to \tau\tau, \mu\mu$ inclusive $gg \to \Phi$ and $gg \to b\bar{b}\Phi$
- $H^\pm \to \nu\tau, tb$ in $pp \to tH^-, W^+H^-, H^+H^-$
- apperance in SUSY cascades [Djouadi et al.]
- no other conclusive way but to find these particles



Bottom-Inclusive Cross Sections



Exclusive production $gg \to \bar{b}tH^-$

– simple example, only one final state bottom jet

→ collinear bottom jets from gluon splitting, regularized by m_b

→ experiment: forward jets, $p_{T,b}$ peaked at m_b

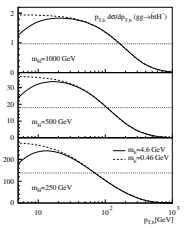
→ use bottom–inclusive cross section

→ possibly large logarithms $\log(p_{T,b}/m_b)$
asymptotic cross section behavior $d\sigma/dp_{T,b} \propto p_{T,b}/m_{T,b}^2$

→ check: plateau in exclusive cross section

→ impact on inclusive rate $\sigma \propto \log[(p_{T,b}^{\max}/m_b)^2 + 1]$

→ how large logarithms? resum?



Inclusive process $bg \to tH^-$

– resum large logarithms $\log(p_{T,b}/m_b)$

– equivalent to bottom parton density
$\mu_{F,b}$ 'transverse momentum size' of bottom parton $(\mu_{F,b} \equiv p_{T,b}^{\max})$

→ usually: hard scale $\mu_{F,b} = M$

→ large enhancement [e.g. $b\bar{b} \to h$]

→ numerical improvement or overestimate?

Bottom Factorization Scale

Two steps: bottom virtuality $Q_b^{\max}$, then transverse momentum $p_{T,b}^{\max}$

– effective $2 \to 2$ cross section: $gg \to \bar{b}X$
hard scale for threshold production $M = M_X = m_H + m_t$

$\to$ (1) approximate steep gluon density $\mathcal{L} = \mathcal{L}_0/x^2$
(2) asymptotic behavior $\overline{|\mathcal{M}|^2} = S^2\sigma_0/Q_b^2$

$$\sigma = \frac{2\sigma_0\mathcal{L}_0}{16\pi} \int_0^{S-M^2} \frac{dQ_b}{Q_b}\, F(Q_b)$$

$\to$ $F(Q_b)$ correction to asymptotic behavior $\quad d\sigma/dQ_b \sim 1/Q_b$

$\to$ turning point $d^2F(Q_b)/d(\log Q_b)^2 = 0 \quad$ at $Q_b^{\max} \sim M/2$

$\to$ translate Q_b into $p_{T,b}$ point by point

$\to$ mostly transverse momentum at threshold $\quad (\rho \equiv p_{z,b}/p_{T,b} \ll 1)$

$$\frac{Q_b^2}{M^2} = \frac{p_{T,b}\sqrt{s}}{M^2}\left(\sqrt{1+\rho^2} - \rho\right) \sim \frac{p_{T,b}}{M}$$

$\to$ $\mu_{F,b} \equiv p_{T,b}^{\max} \sim Q_b^{\max}/2 \sim M/4$

$\to$ numerical study of $gg \to \bar{b}tH^-$: $\quad \mu_{F,b} \sim M/5$

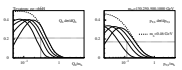
So what did we learn from exclusive process?

– 'large' logs at maximum $\log(M/(4m_b))$

– hard scale for inclusive process: $\quad \mu_{F,b} \propto M$

– gg and bg processes: $\quad \mu_{F,b} \sim M/4$ from partonic phase space

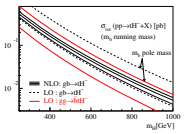
– valid for Tevatron and LHC

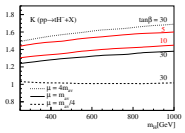


QCD Corrections to Inclusive Channel

Next-to-leading Order QCD Calculation:

- leading order uncertainty large for $bg \to tH^-$
  e.g. mass definition: $\overline{MS}$ or pole mass for $y_{b,t}$?
- complete set of virtual and real SUSY corrections
- running top and bottom Yukawa coupling

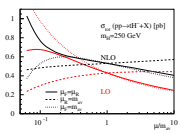




$\to$ NLO correction $+30\% \cdots 40\%$ perturbatively stable [Zhu]

Scale Dependence in NLO:

- generic cancellations for $\mu_R \equiv \mu_F$ [Harlander & Kilgore]
- renormalization scale dependence numerically dominant
  $\mu_R \sim (m_t + m_H)/2$ natural choice [c.f. Higgs decays, Melnikov]
- factorization scale dependene critical only for $\mu_F \sim m_b$
  $\mu_F \sim (m_t + m_H)/5$ from exclusive process

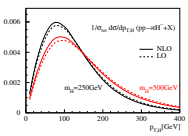


$\to$ NLO scale dependence $\pm 20\%$

$\to$ well defined limit $\mu_F \to m_b$ returns exclusive process at NLO

Distributions in NLO:

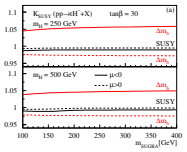
- Higgs transverse momentum softened (gluon density)
- Higgs rapidity not symmetric (gluon splitting)



SUSY-QCD Corrections

SUSY-QCD Loop Contributions:

- infrared finite but ultraviolet divergent SUSY loops
- parameterized by $K_{\rm SUSY} = 1 + \sigma_{\rm SUSY}/\sigma_{\rm NLO}$
- (1) universal corrections $y_b \to y_b/(1+\Delta m_b)$
  [Carena, Garcia, Nierste, Wagner]



- (2) remaining explicit SUSY loop diagrams [Gao, Lu, Xiong, Yang]

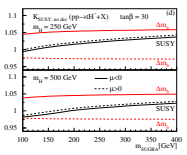
$\to$ Δm_b corrections dominant for $\tan\beta \gtrsim 10$ (dependent on sign of μ)

$\to$ explicit loop corrections negligible $\lesssim 5\%$ for generic mSUGRA

Decoupling of Running Parameters: $\alpha_s(\mu_R), y_{b,t}(\mu_R)$

- heavy SUSY particle loops ultraviolet divergent

$\to$ SUSY counter terms for Standard Model parameters



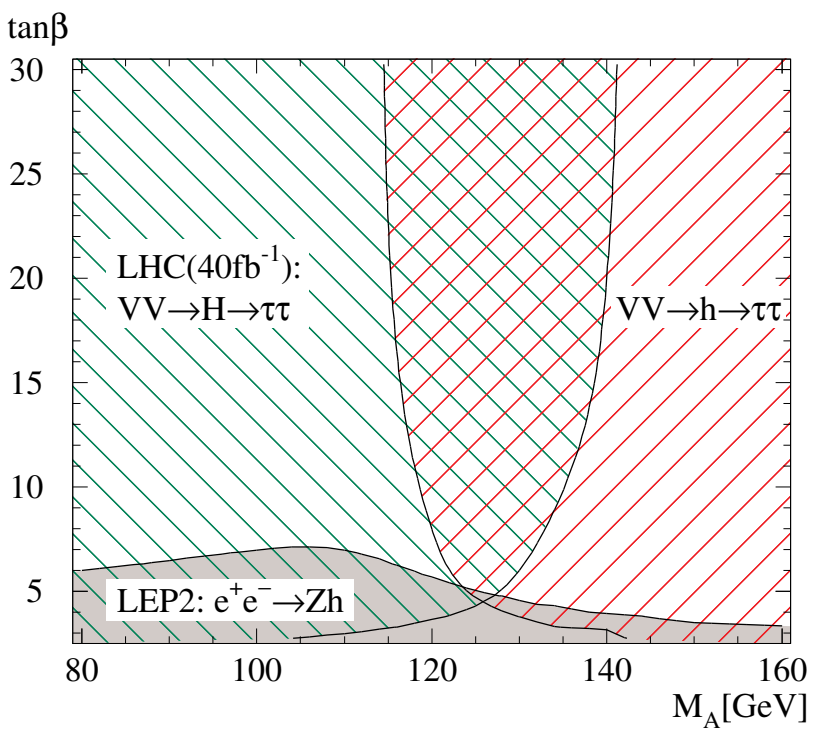
$\to$ SUSY contributions to beta functions

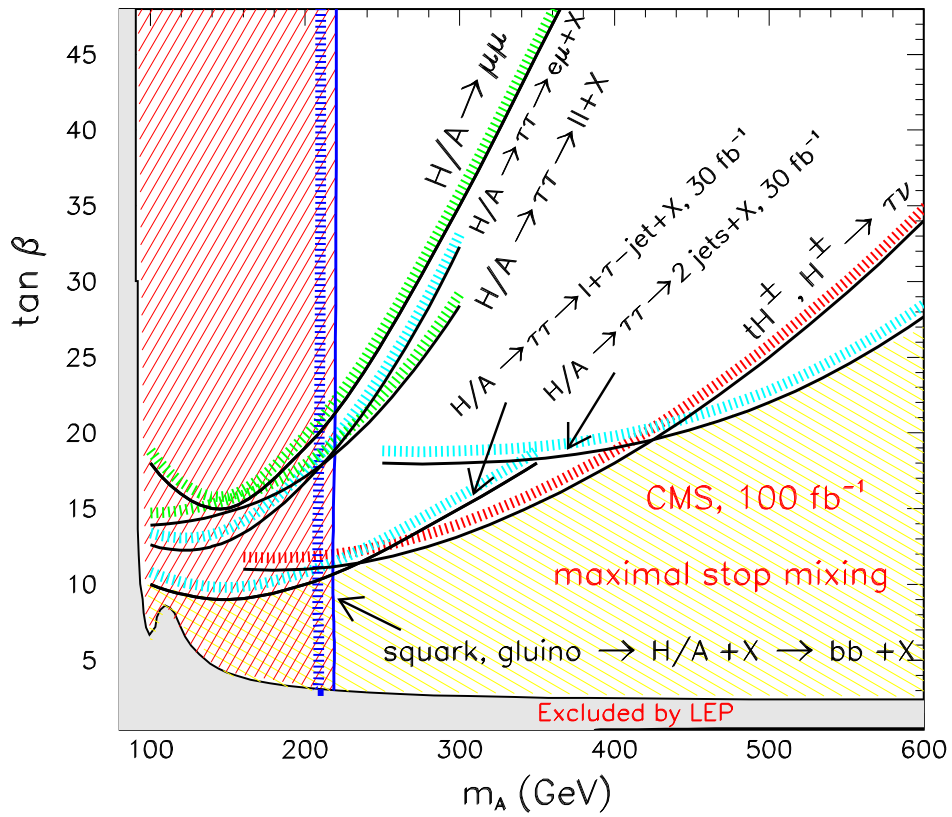
$\to$ explicit decoupling necessary:
$m_{b,t}(\mu_R) \to m_{b,t}(\mu_R)[1 + \alpha_s/(4\pi) C_F \log(\mu_R^2/m^2_{\rm heavy})]$

Conclusions

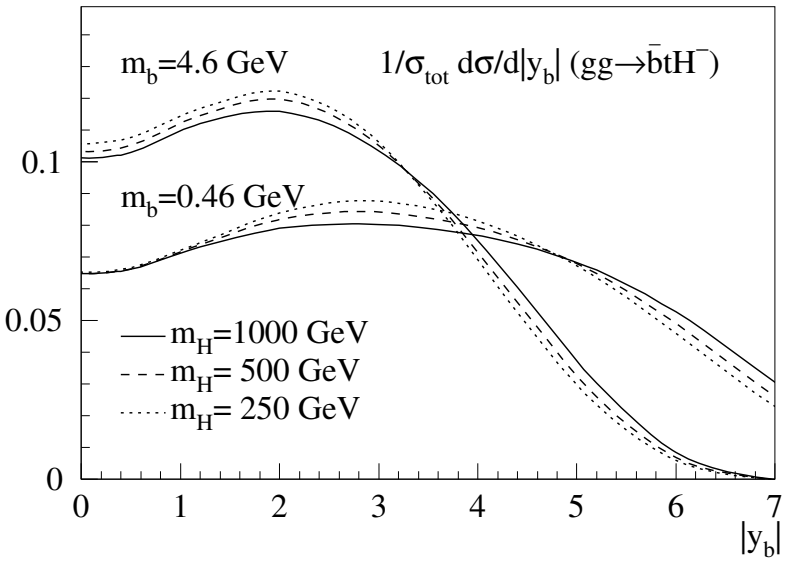
- heavy Higgs bosons necessary to tell it might be the MSSM
- bottom initiated process $bg \to tH^-$ appropriate
  with factorization scale generally $\mu_{F,b} \sim M/5$
- NLO_1: inclusive process well defined
  NLO_2: $30\% \cdots 40\%$ enhancement of σ_{tot} in 2HDM
  NLO_3: remaining scale uncertainty $\lesssim 20\%$
  NLO_4: Δm_b corrections dominant in MSSM for large $\tan\beta$
  NLO_5: non-factorizable corrections negligible in MSSM

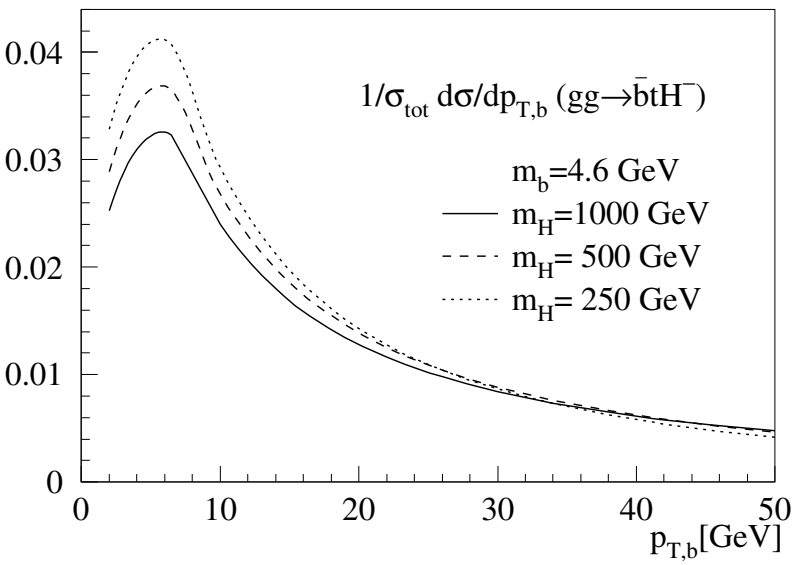
thanks to Kyle Cranmer for printing this talk on *almost* a CERN holiday

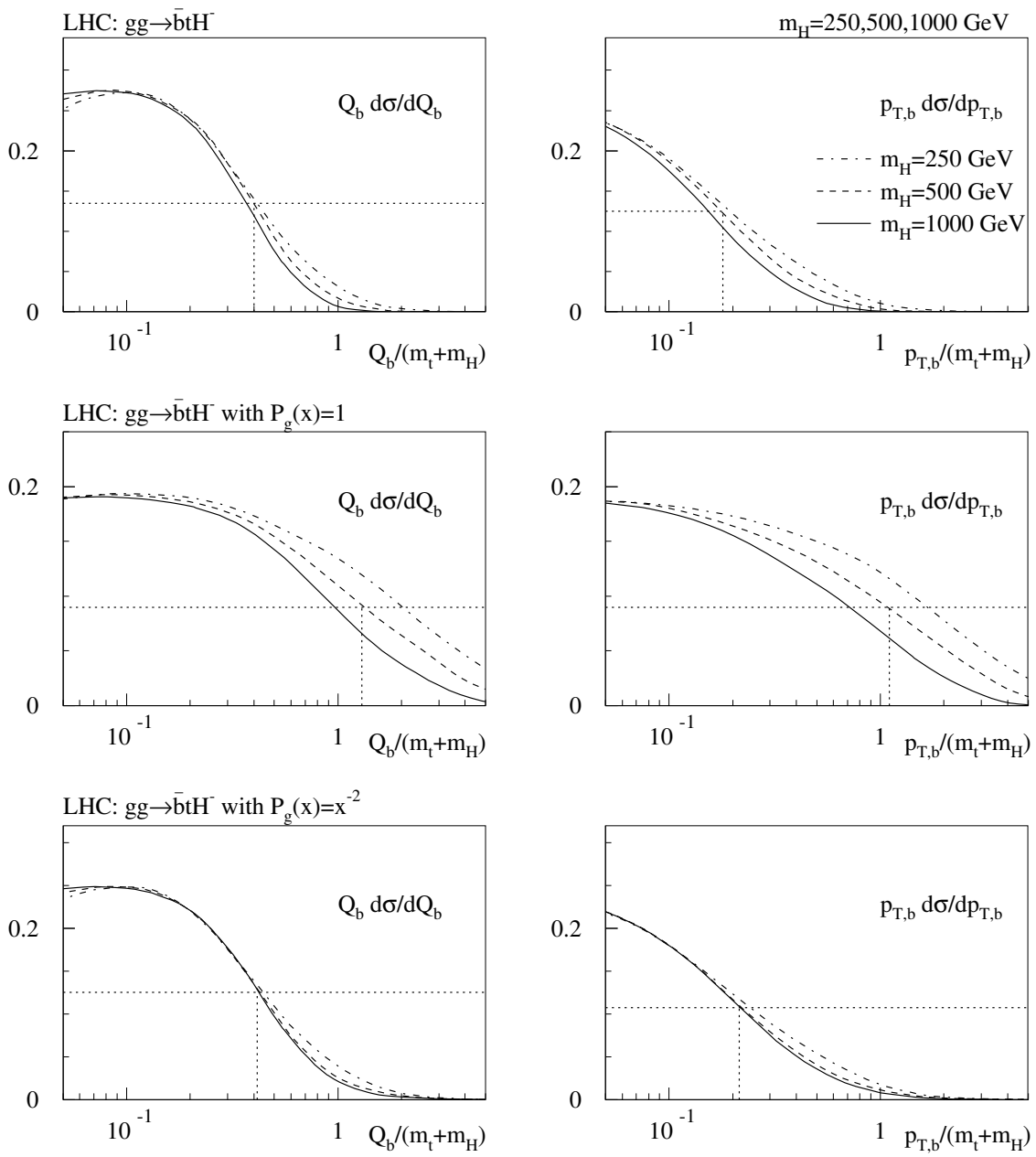

tanβ
30
25
20
15
10
5
LHC(40fb-1):
VV→H→ττ
VV→h→ττ
LEP2: e+e−→Zh
80
100
120
140
160
MA[GeV]

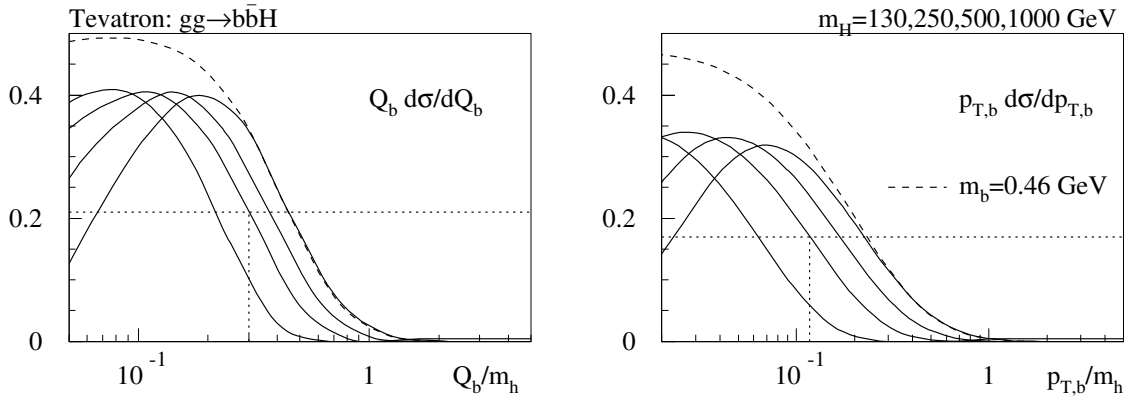


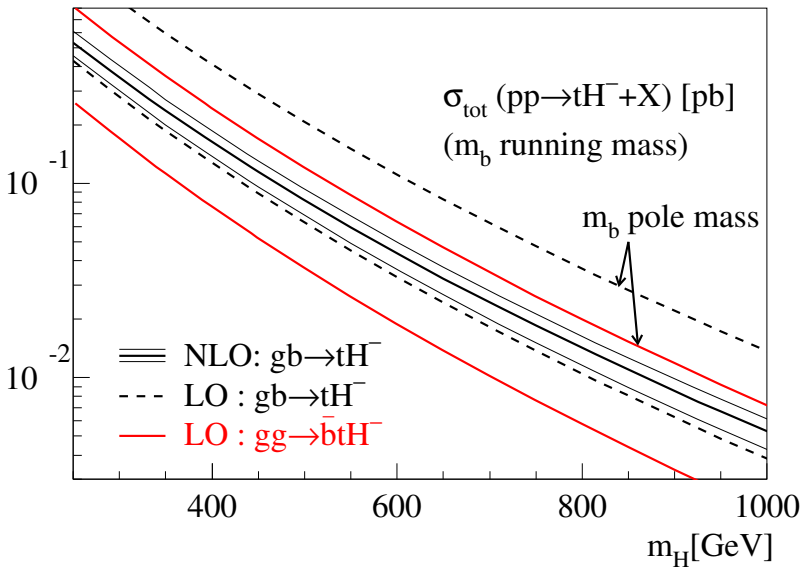
Datta, Djouadi, Guchait, Moortgat

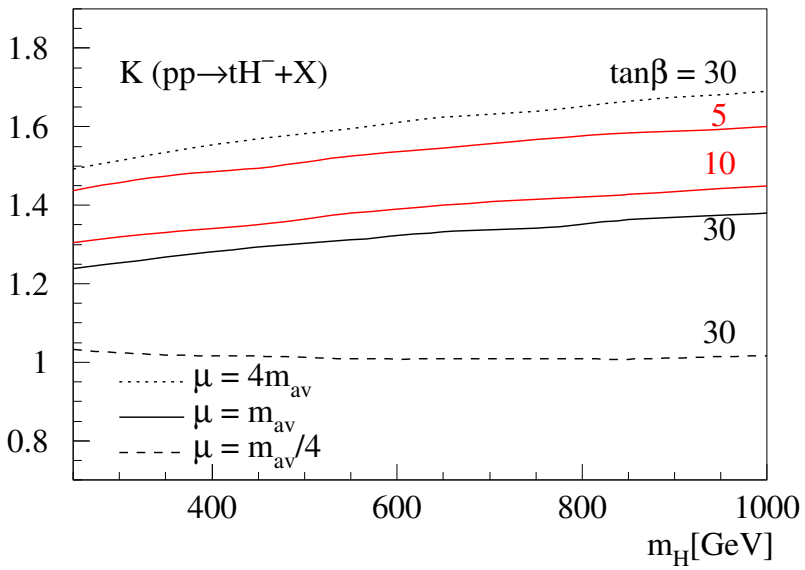

m_b=4.6 GeV
$1/\sigma_{tot}\ d\sigma/d|y_b|\ (gg\to\bar{b}tH^-)$
m_b=0.46 GeV
m_H=1000 GeV
m_H= 500 GeV
m_H= 250 GeV
0.1
0.05
0
0
1
2
3
4
5
6
7
$|y_b|$

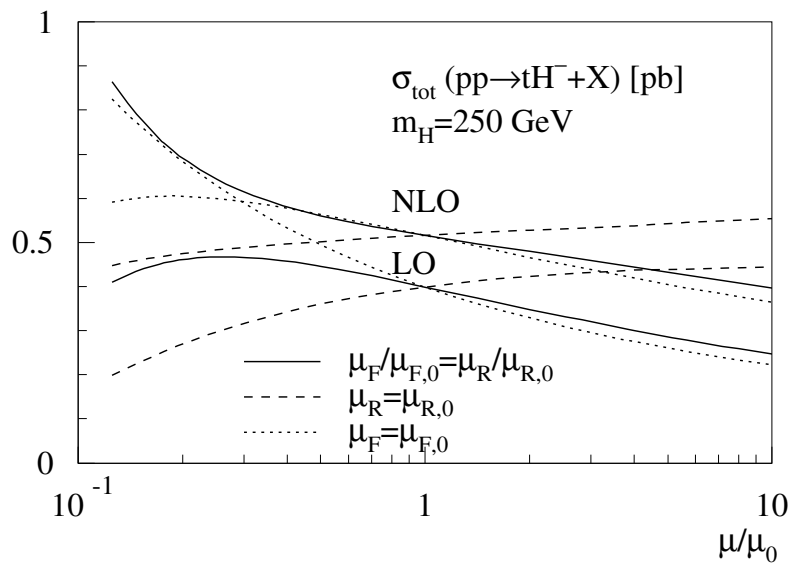

$1/\sigma_{tot}\ d\sigma/dp_{T,b}\ (gg\to\bar{b}tH^-)$
m_b=4.6 GeV
m_H=1000 GeV
m_H= 500 GeV
m_H= 250 GeV
0.04
0.03
0.02
0.01
0
0
10
20
30
40
50
$p_{T,b}$[GeV]

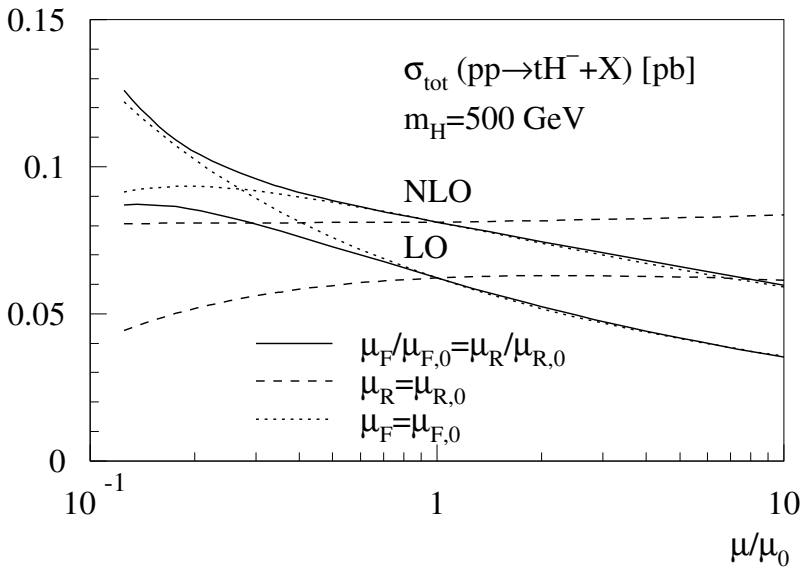

LHC: gg→b̄tH⁻
m_H=250,500,1000 GeV
Q_b dσ/dQ_b
p_T,b dσ/dp_T,b
m_H=250 GeV
m_H=500 GeV
m_H=1000 GeV
0.2
0
10^-1
1
Q_b/(m_t+m_H)
p_T,b/(m_t+m_H)
LHC: gg→b̄tH⁻ with P_g(x)=1
LHC: gg→b̄tH⁻ with P_g(x)=x^-2

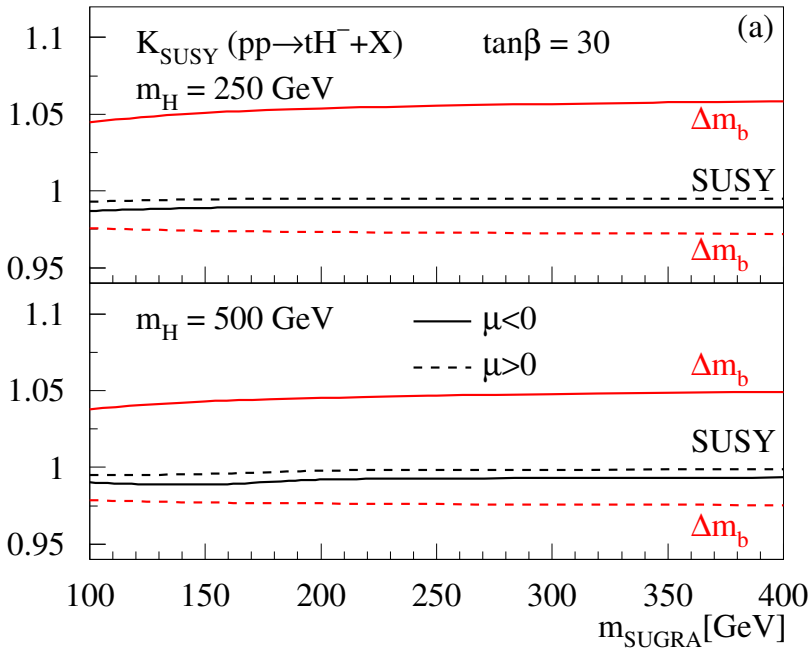

Tevatron: gg→bb̄H
$Q_b\, d\sigma/dQ_b$
0.4
0.2
0
10^{-1}
1
Q_b/m_h
m_H=130,250,500,1000 GeV
$p_{T,b}\, d\sigma/dp_{T,b}$
m_b=0.46 GeV
0.4
0.2
0
10^{-1}
1
$p_{T,b}/m_h$

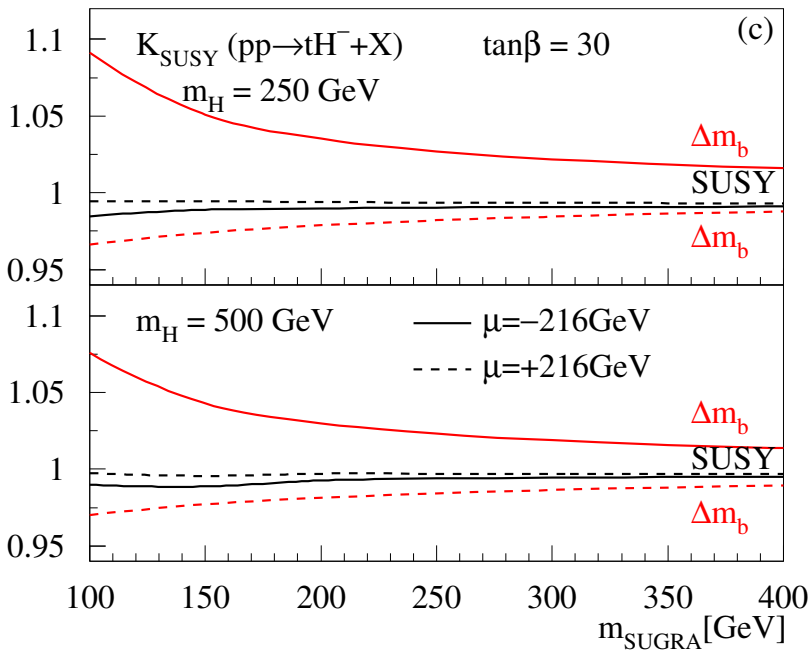

σ_{tot} (pp→tH⁻+X) [pb]
(m_b running mass)
m_b pole mass
NLO: gb→tH⁻
LO : gb→tH⁻
LO : gg→$\bar{b}$tH⁻
10^{-1}
10^{-2}
400
600
800
1000
m_H[GeV]


K (pp→tH⁻+X)
tanβ = 30
5
10
30
30
μ = 4m_{av}
μ = m_{av}
μ = m_{av}/4
1.8
1.6
1.4
1.2
1
0.8
400
600
800
1000
m_H[GeV]


1
0.5
0
σ_{tot} (pp→tH⁻+X) [pb]
m_H=250 GeV
NLO
LO
$\mu_F/\mu_{F,0}=\mu_R/\mu_{R,0}$
$\mu_R=\mu_{R,0}$
$\mu_F=\mu_{F,0}$
10^{-1}
1
10
μ/μ_0


0.15
0.1
0.05
0
σ_{tot} (pp→tH⁻+X) [pb]
m_H=500 GeV
NLO
LO
$\mu_F/\mu_{F,0}=\mu_R/\mu_{R,0}$
$\mu_R=\mu_{R,0}$
$\mu_F=\mu_{F,0}$
10^{-1}
1
10
μ/μ_0


(a)
K_{SUSY} ($pp \to tH^- + X$)
tanβ = 30
m_H = 250 GeV
Δm_b
SUSY
Δm_b
m_H = 500 GeV
μ<0
μ>0
Δm_b
SUSY
Δm_b
1.1
1.05
1
0.95
100
150
200
250
300
350
400
m_{SUGRA}[GeV]


(c)
K_{SUSY} ($pp \to tH^- + X$)
tanβ = 30
m_H = 250 GeV
Δm_b
SUSY
Δm_b
m_H = 500 GeV
μ=−216GeV
μ=+216GeV
Δm_b
SUSY
Δm_b
1.1
1.05
1
0.95
100
150
200
250
300
350
400
m_{SUGRA}[GeV]