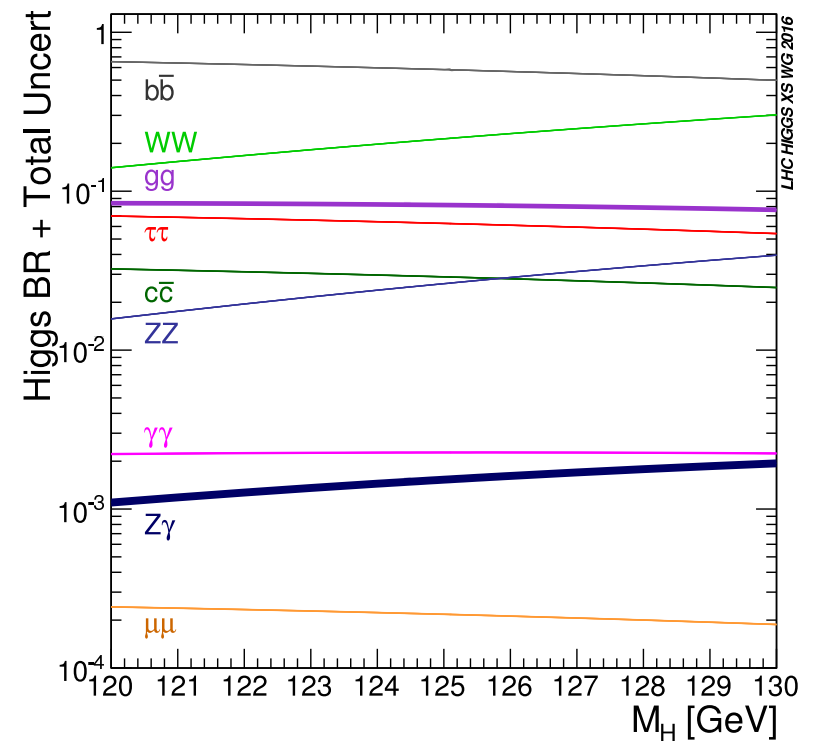
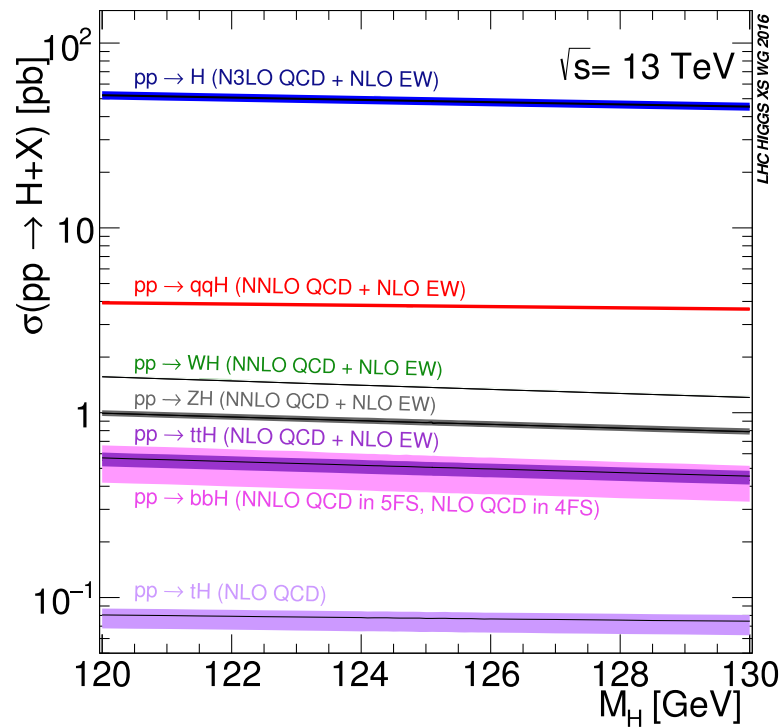
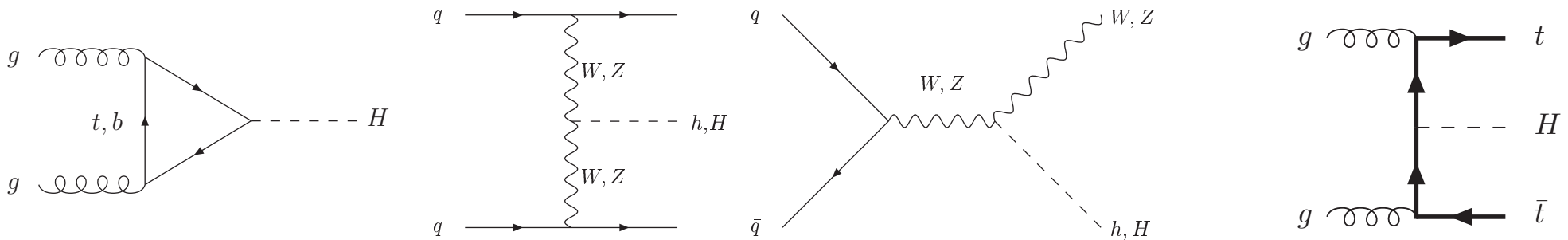
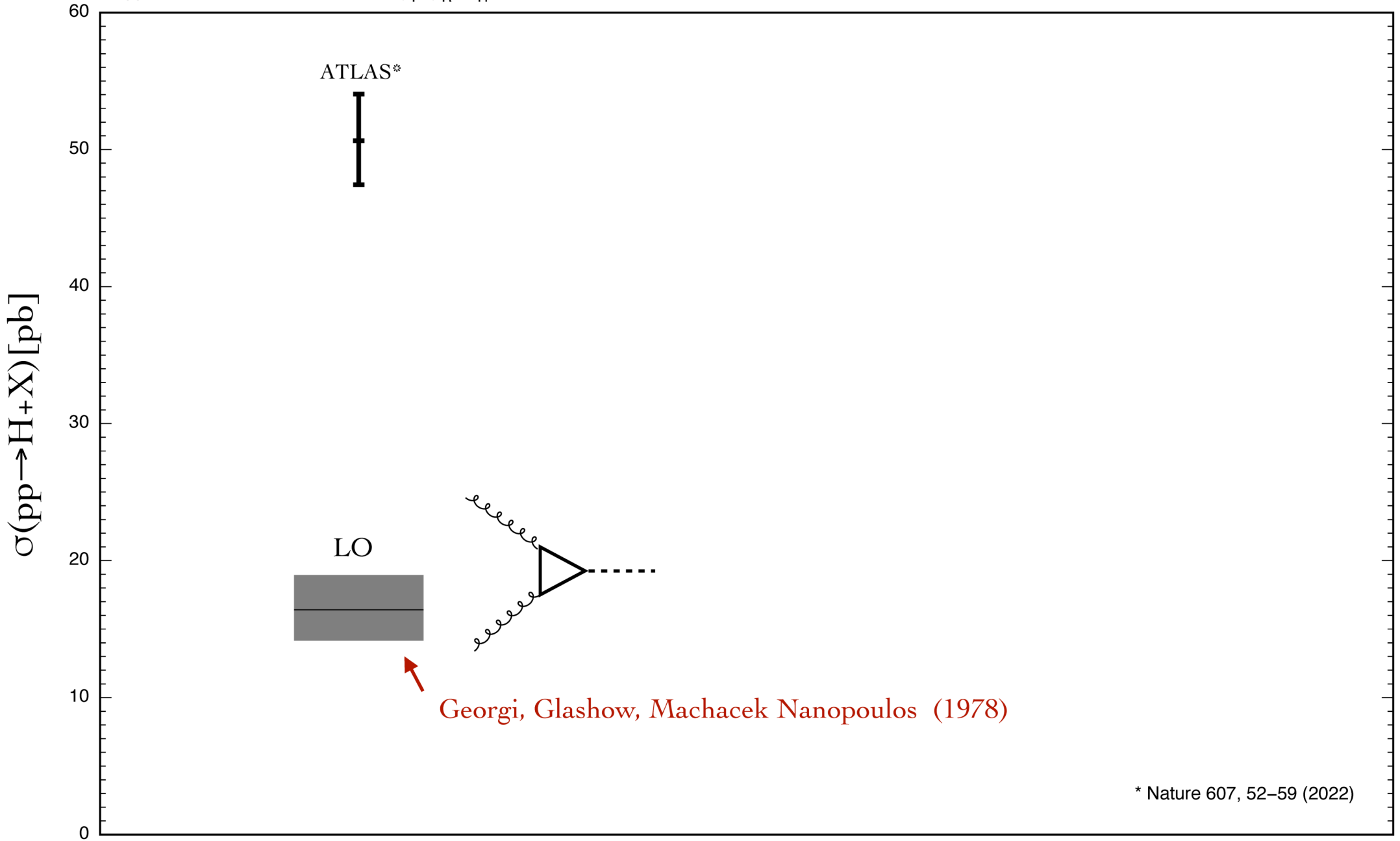
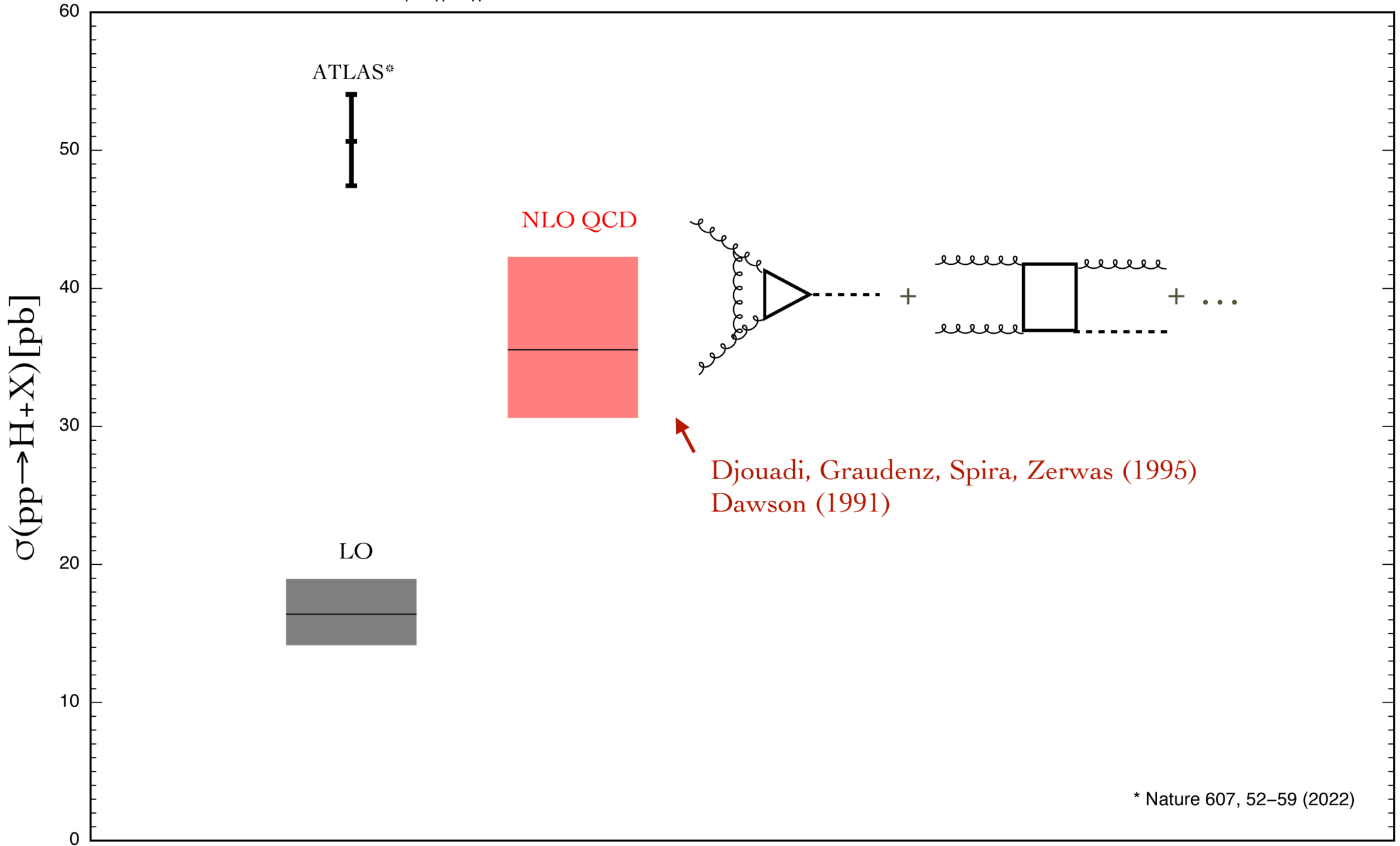


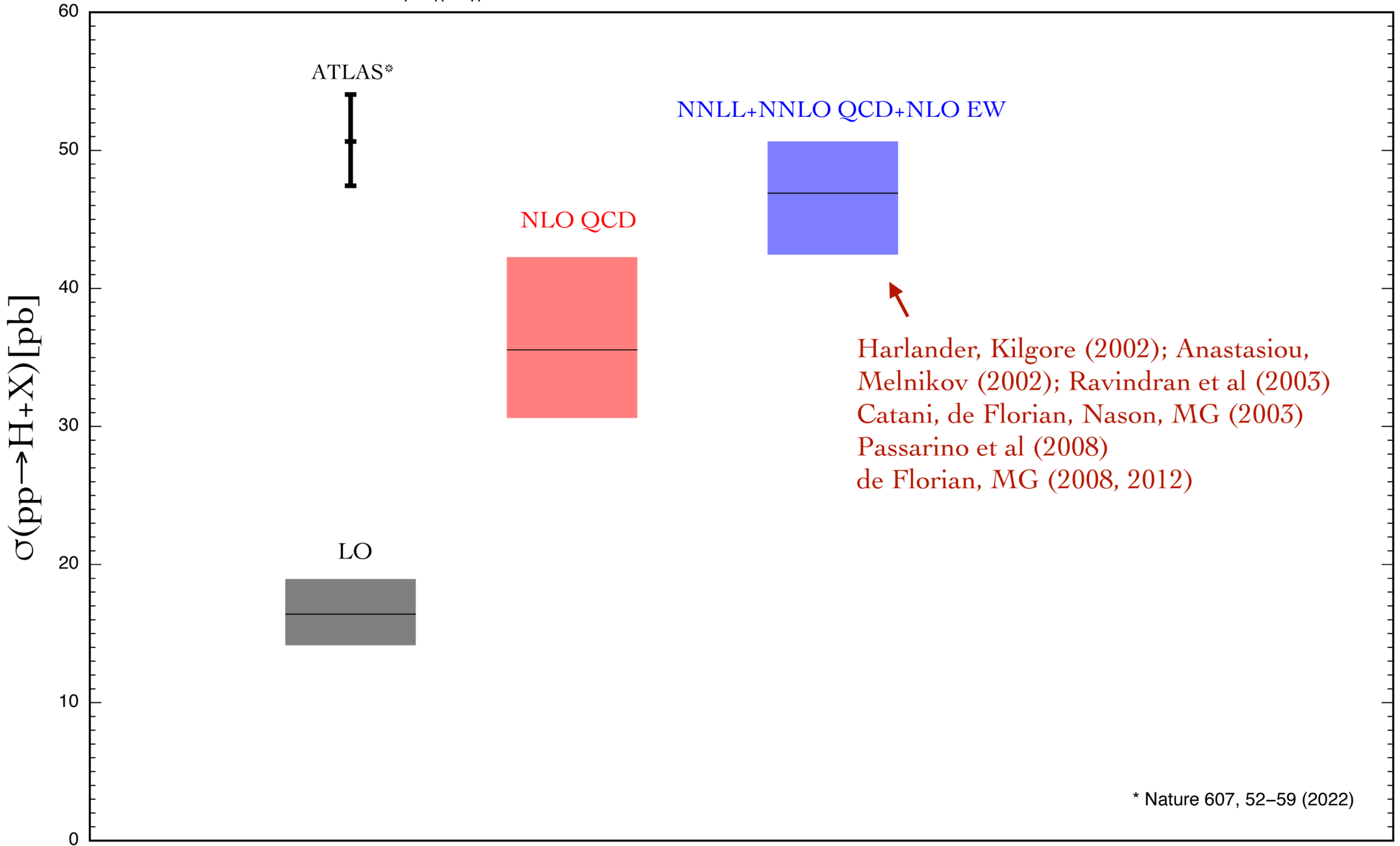
I INTRODUCTION

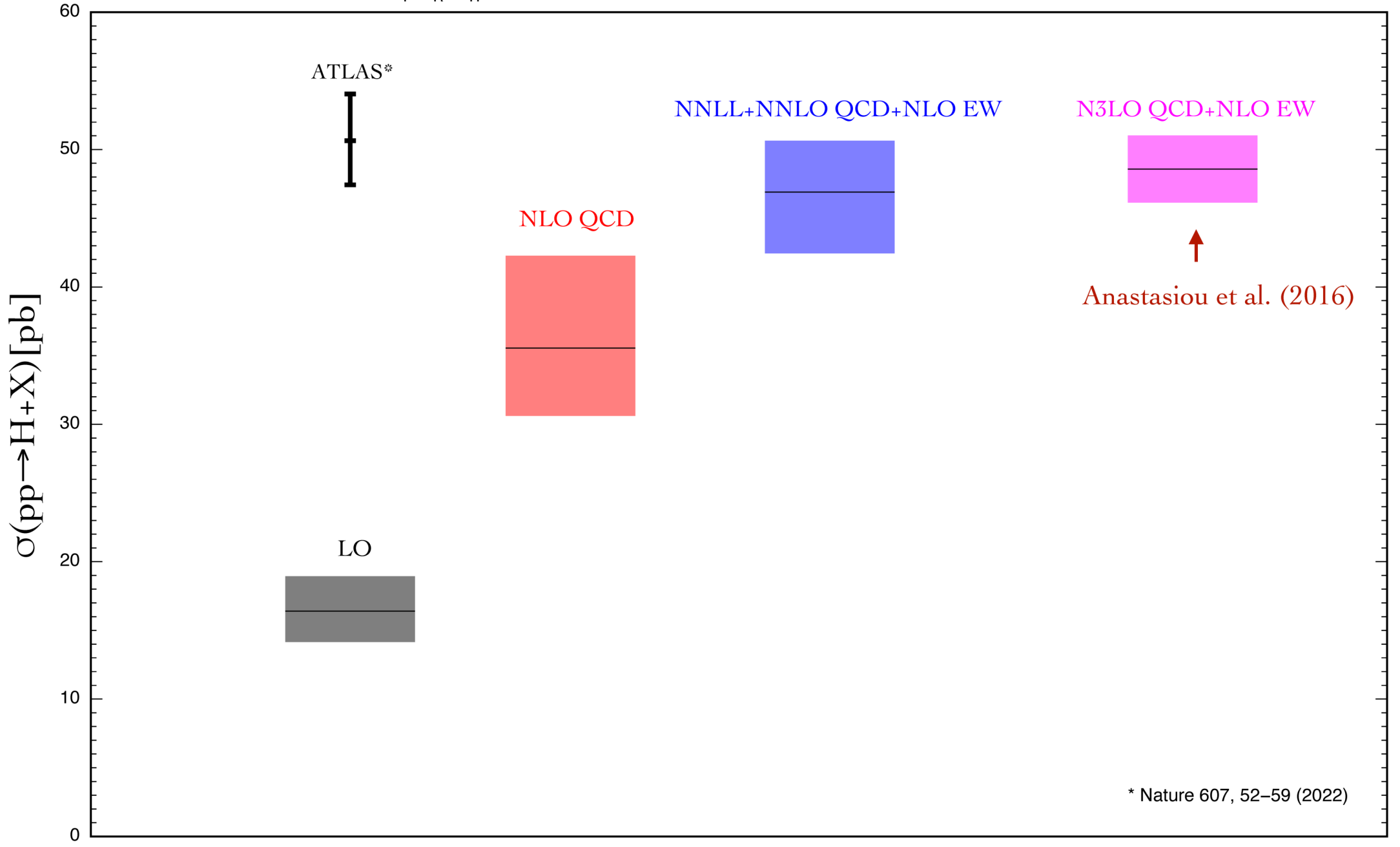
• Higgs Boson Production



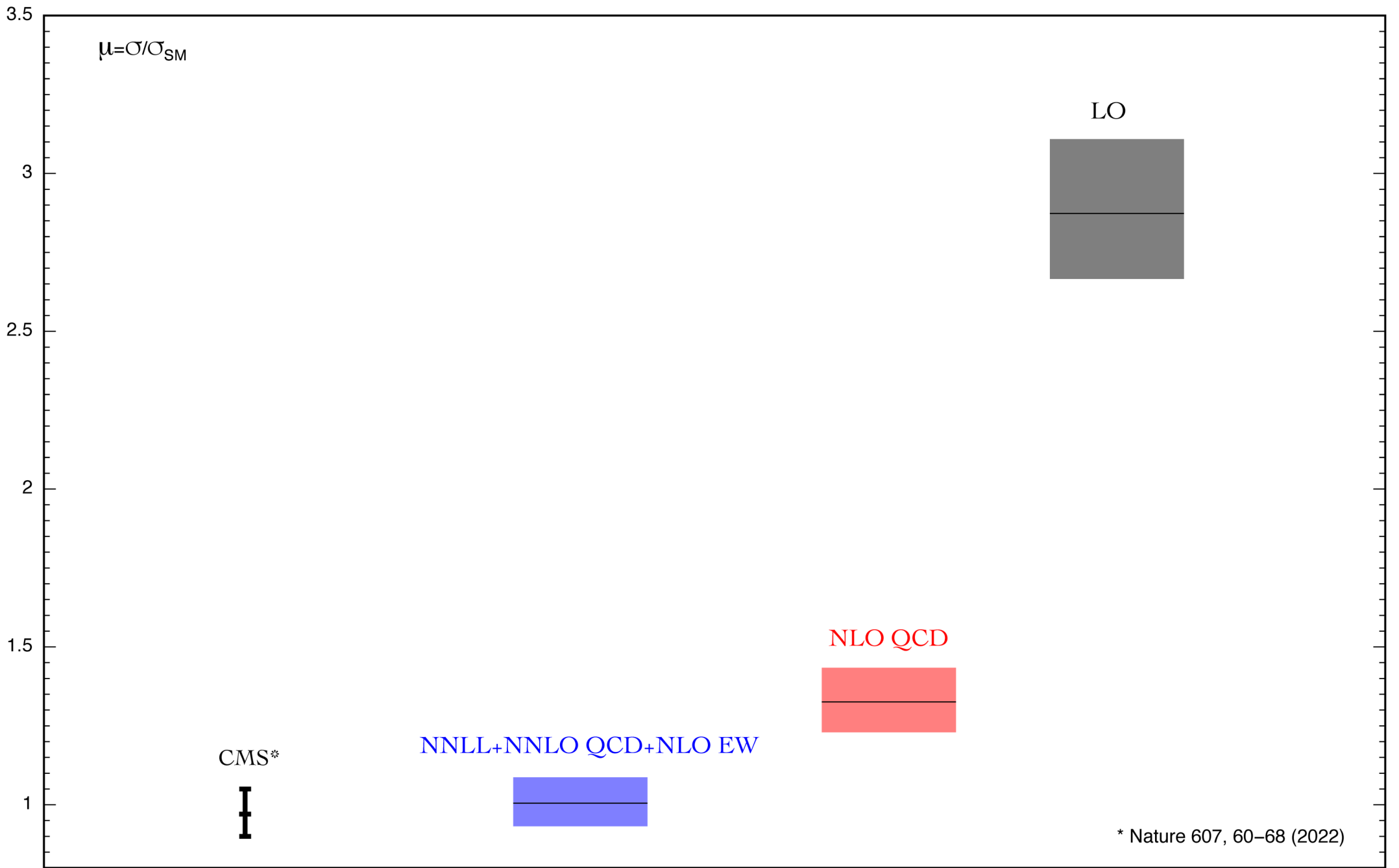






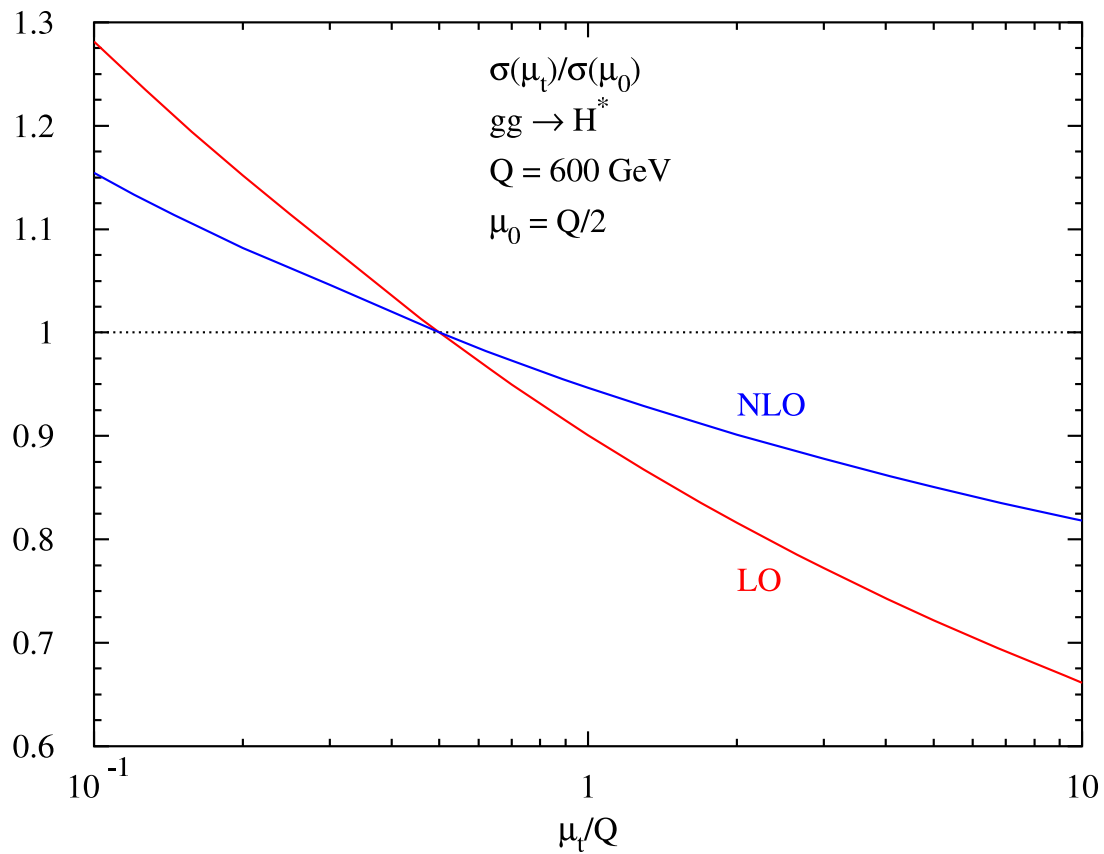


* Nature 607, 52–59 (2022)



$$\sigma(gg \rightarrow H)_{LO} = 18.43^{+0.8\%}_{-1.1\%} \text{ pb}$$

$$\sigma(gg \rightarrow H)_{NLO}^{QCD} = 42.17^{+0.4\%}_{-0.5\%} \text{ pb}$$



Jones, S.

$$\sigma(gg \rightarrow H_{SM}^*) \equiv \sigma(gg \rightarrow H_{BSM}) \Big|_{M_{H_{BSM}}=Q}$$

- m_t scheme/scale uncertainties only:

- LO:

$$\sigma(gg \rightarrow H^*)|_{Q=125 \text{ GeV}} = 18.43^{+0.8\%}_{-1.1\%} \text{ pb}, \quad \sigma(gg \rightarrow H^*)|_{Q=300 \text{ GeV}} = 4.88^{+23.1\%}_{-1.1\%} \text{ pb}$$

$$\sigma(gg \rightarrow H^*)|_{Q=400 \text{ GeV}} = 4.94^{+1.2\%}_{-1.8\%} \text{ pb}, \quad \sigma(gg \rightarrow H^*)|_{Q=600 \text{ GeV}} = 1.13^{+0.0\%}_{-26.2\%} \text{ pb}$$

$$\sigma(gg \rightarrow H^*)|_{Q=900 \text{ GeV}} = 0.139^{+0.0\%}_{-36.0\%} \text{ pb}, \quad \sigma(gg \rightarrow H^*)|_{Q=1200 \text{ GeV}} = 0.0249^{+0.0\%}_{-41.1\%} \text{ pb}$$

- NLO QCD:

$$\sigma(gg \rightarrow H^*)|_{Q=125 \text{ GeV}} = 42.17^{+0.4\%}_{-0.5\%} \text{ pb}, \quad \sigma(gg \rightarrow H^*)|_{Q=300 \text{ GeV}} = 9.85^{+7.5\%}_{-0.3\%} \text{ pb}$$

$$\sigma(gg \rightarrow H^*)|_{Q=400 \text{ GeV}} = 9.43^{+0.1\%}_{-0.9\%} \text{ pb}, \quad \sigma(gg \rightarrow H^*)|_{Q=600 \text{ GeV}} = 1.97^{+0.0\%}_{-15.9\%} \text{ pb}$$

$$\sigma(gg \rightarrow H^*)|_{Q=900 \text{ GeV}} = 0.230^{+0.0\%}_{-22.3\%} \text{ pb}, \quad \sigma(gg \rightarrow H^*)|_{Q=1200 \text{ GeV}} = 0.0402^{+0.0\%}_{-26.0\%} \text{ pb}$$

⇒ limited sensitivity to interference effects!

$$\sigma = \sigma_{H_1} + \Delta\sigma_{int} + \sigma_{H_2}$$

[BTW: very difficult to determine charm Yukawa coupl. from charm loops in p_{TH} distribution ($H + j$)

Bishara, Haisch, Monni, Re

- different radiative corrections to top and bottom loops [pole masses]:

$$\sigma(gg \rightarrow H) = \sigma_{tt} + \sigma_{tb} + \sigma_{bb}$$

$$K_{tt} \sim 1.68$$

$$K_{tb} \sim 0.97$$

$$K_{bb} \sim 1.20$$

⇒ up to 20 – 30% differences in NLO cxn [m_b : scheme/scale dep.?)

⇒ not possible to use SM-like cxns in many BSM cases

for different weighting of top and bottom loops

[enhancement of bottom loops (e.g. 2HDM type II, MSSM, . . .)]

- bottom-loop dominance: full NLO 20% uncertainties ← double logs

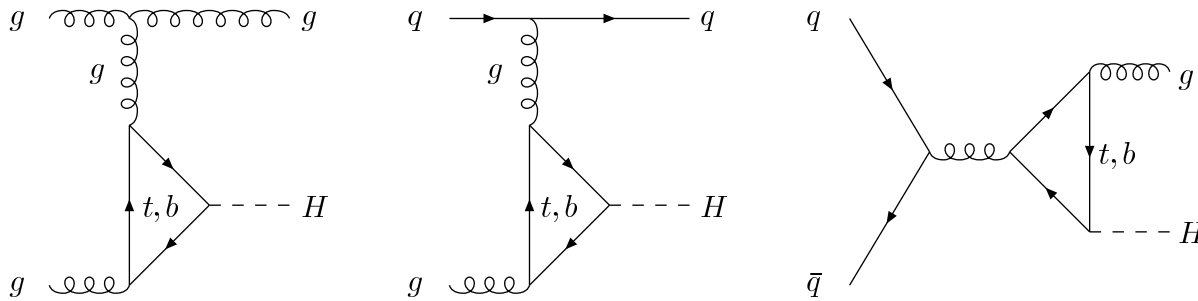
- can only use N³LO results for σ_{tt}

⇒ individual grids [(pseudo)scalar] for $\sigma_{tt}, \sigma_{tb}, \sigma_{bb}$ [← σ_{BSM} ?]

- BSM heavy: eff. ggH coupl. $c_g \rightarrow$ interf. with full top/bottom loops!

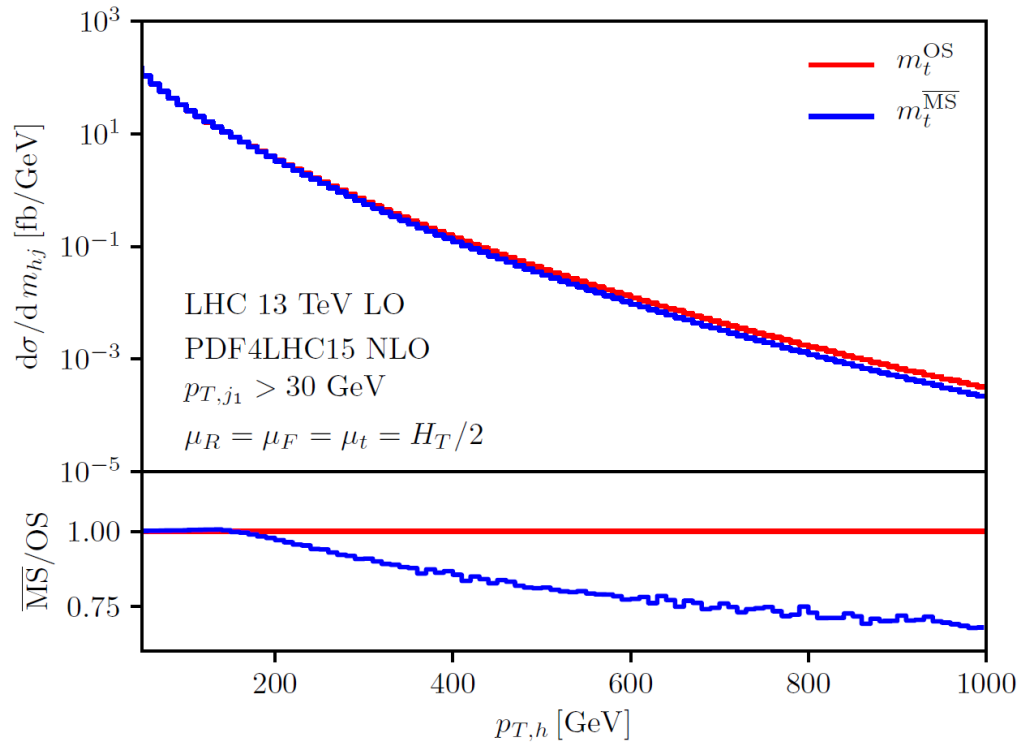
$$\sigma(gg \rightarrow H) = \underbrace{\sigma_{c_g c_g}}_{\sim N^3 LO} + \underbrace{\sigma_{tt} + \sigma_{tb} + \sigma_{bb}}_{NLO} + \underbrace{\sigma_{c_g t}}_{\sim N^3 LO} + \underbrace{\sigma_{c_g b}}_{NLO} \quad \left[\mathcal{L}_{BSM} = c_g G^{a\mu\nu} G_{\mu\nu}^a H \right]$$

• Higgs + jet production: $gg \rightarrow H + j$



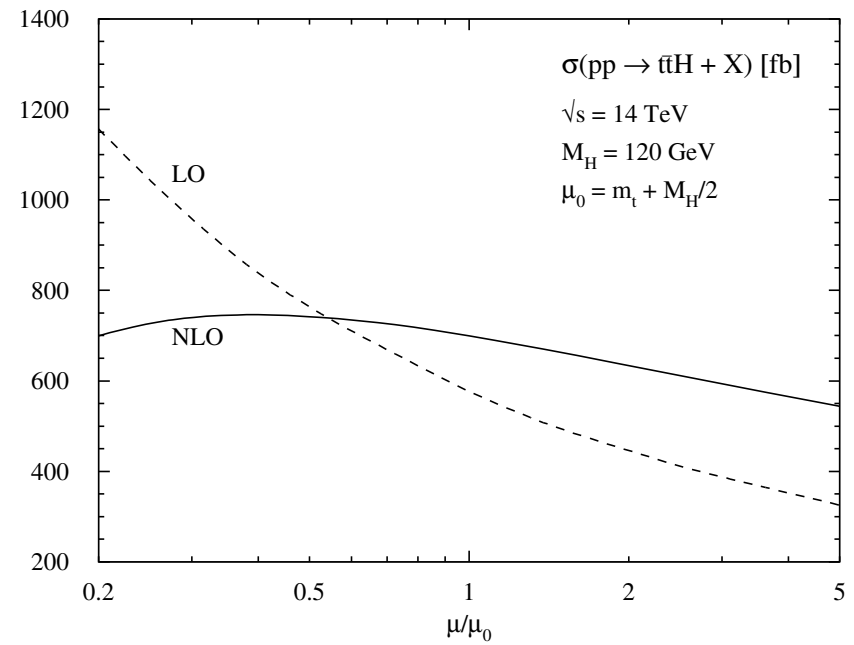
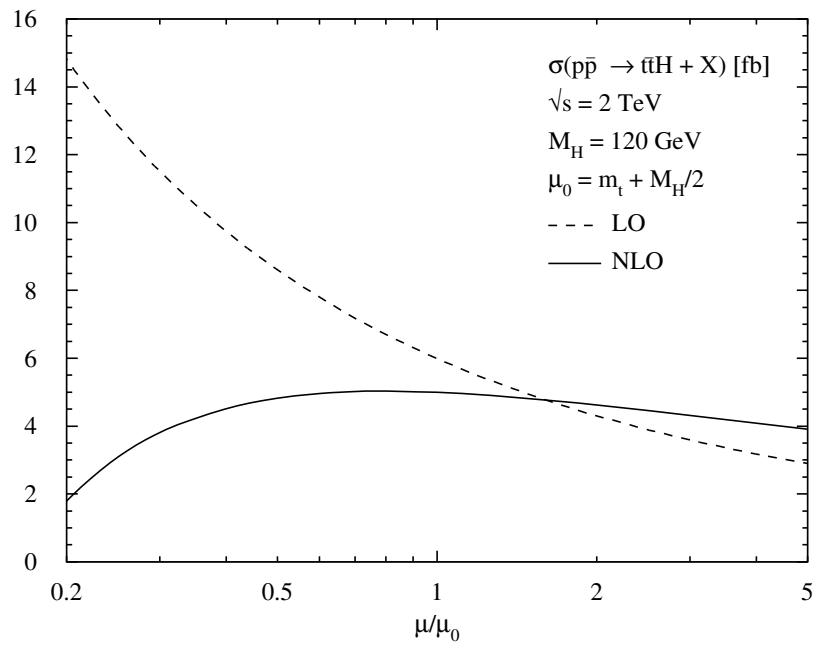
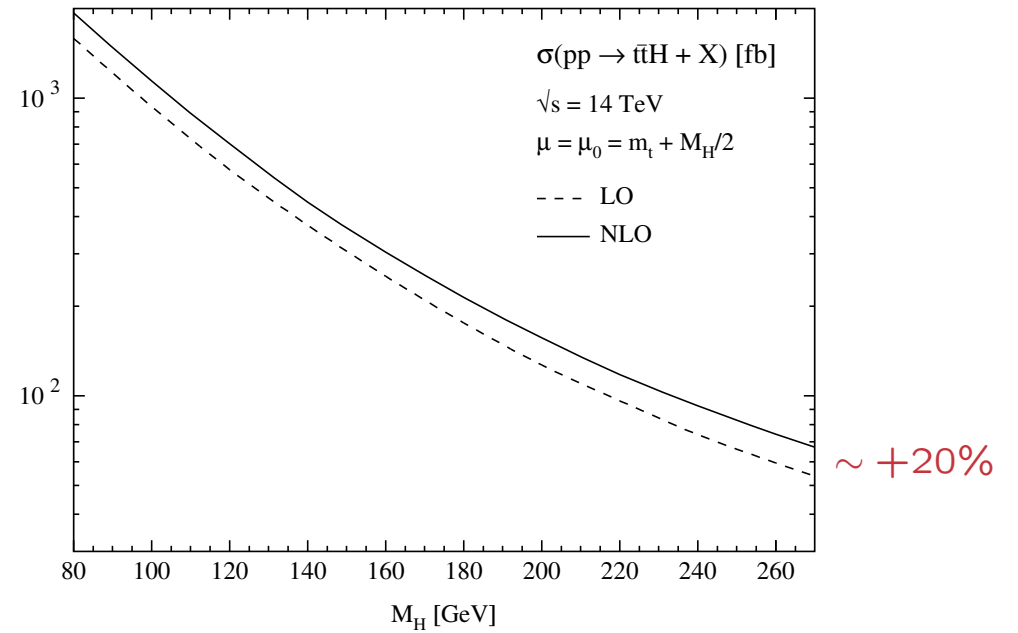
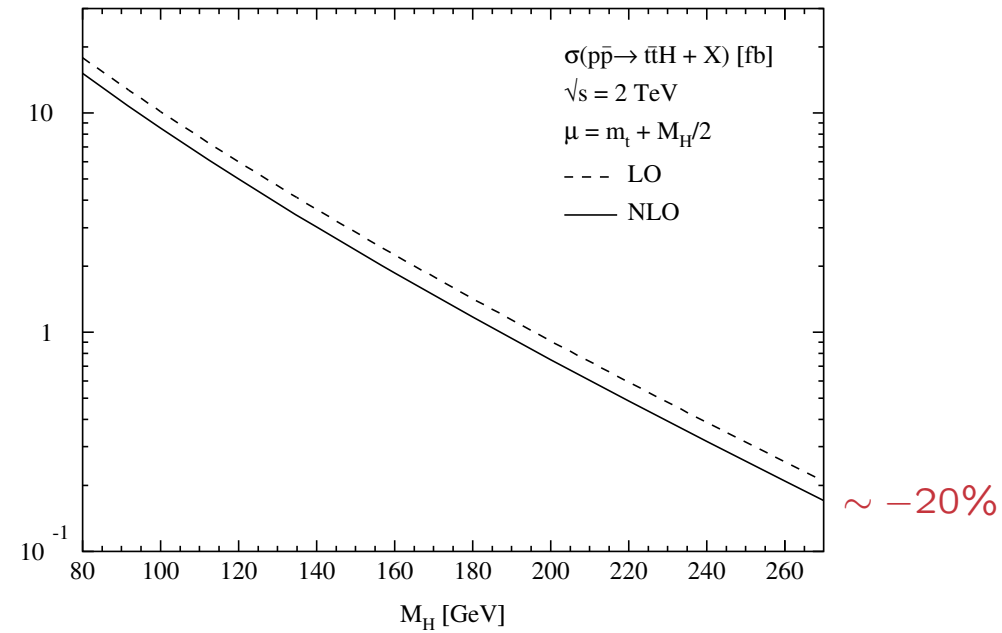
$$\text{LO: } \mu_t = H_T/2 = (\sqrt{M_H^2 + p_T^2} + p_{Tj})/2$$

$pp \rightarrow H + j$



→ NLO? Jones, Kerner, Luisoni

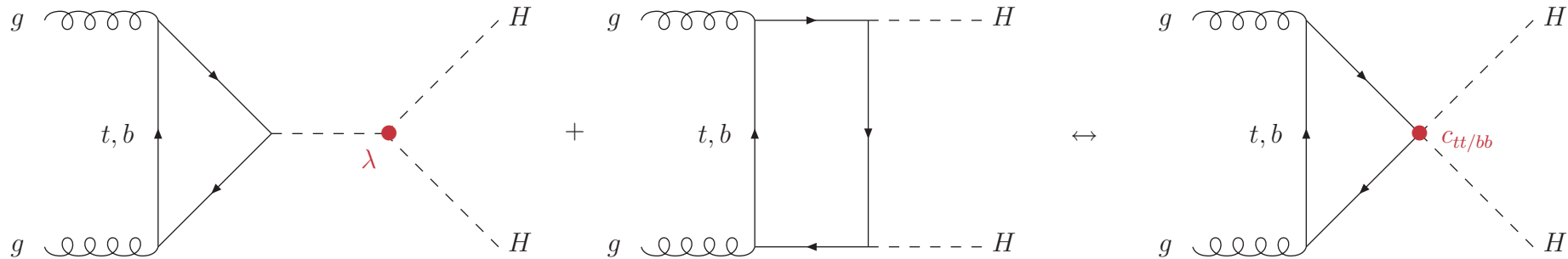
Jones, S.



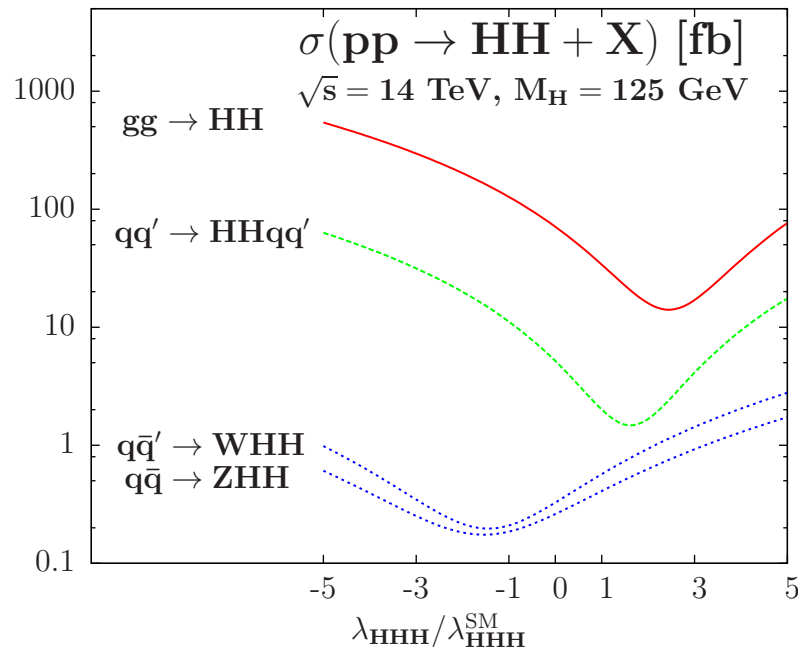
Beenakker, Dittmaier, Krämer, Plümper, S., Zerwas

- full agreement with Dawson, Orr, Reina, Wackerroth

(v) $gg \rightarrow HH$



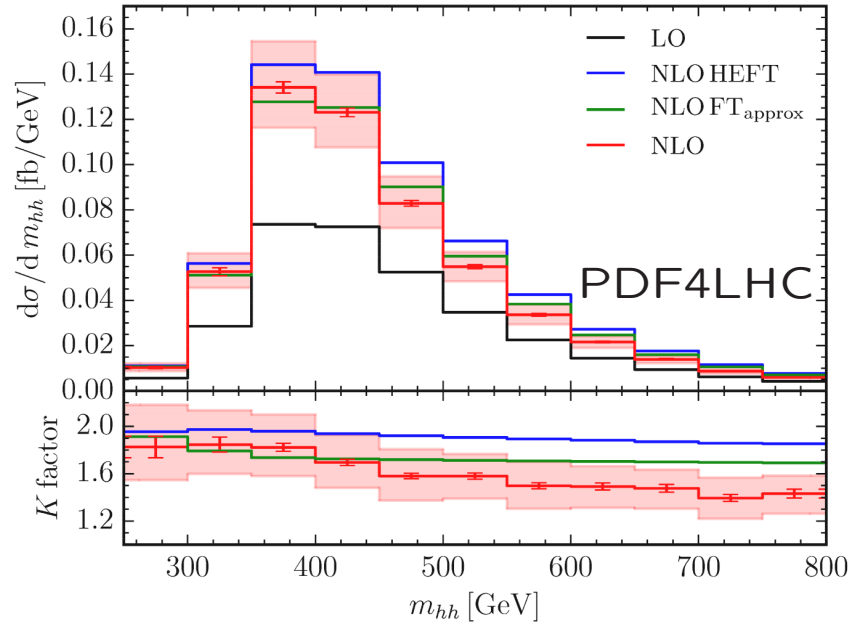
- threshold region: sensitive to λ
- large M_{HH} : sensitive to $c_{tt/bb}$ [e.g. boosted Higgs pairs]



$$gg \rightarrow HH : \frac{\Delta\sigma}{\sigma} \sim -\frac{\Delta\lambda}{\lambda}$$

[decreasing with M_{HH}^2]

Baglio, Djouadi, Gröber, Mühlleitner, Quevillon, S.



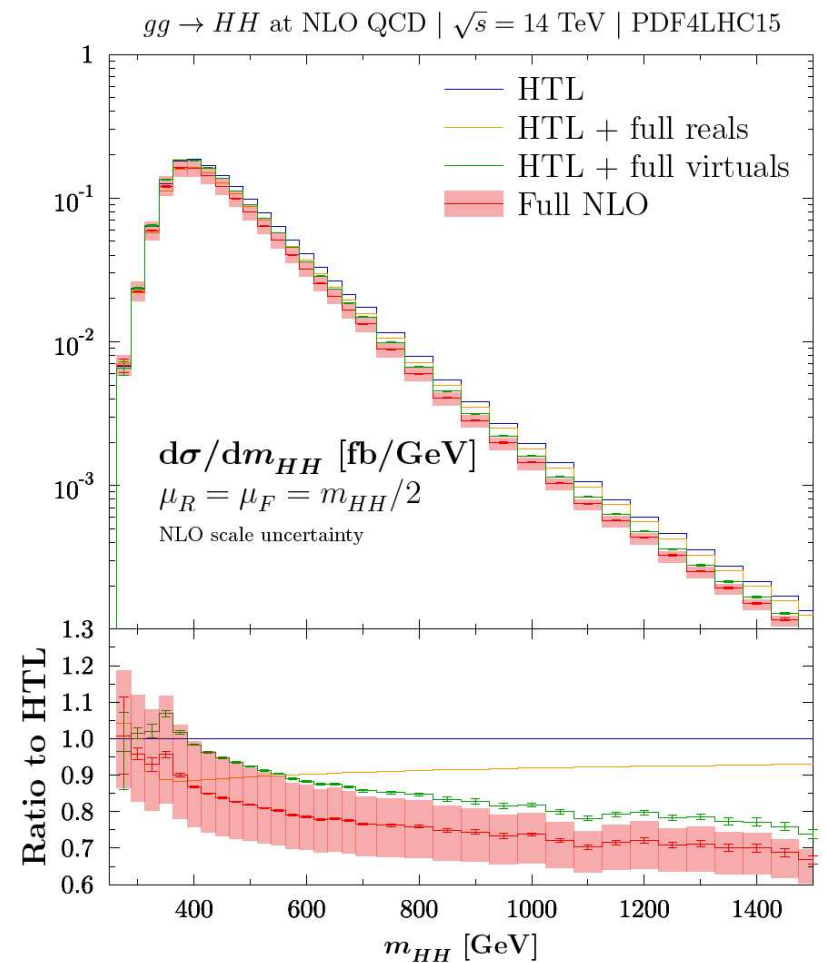
Borowka, Greiner, Heinrich, Jones, Kerner
Schlenk, Schubert, Zirke

$$\sigma_{NLO} = 32.91(10)_{-12.8\%}^{+13.8\%} \text{ fb}$$

$$\sigma_{NLO}^{HTL} = 38.75_{-15\%}^{+18\%} \text{ fb}$$

$$m_t = 173 \text{ GeV}$$

⇒ -15% mass effects on top of LO



Baglio, Campanario, Glaus,
Mühlleitner, Ronca, S., Streicher

$$\sigma_{NLO} = 32.81(7)_{-12.5\%}^{+13.5\%} \text{ fb}$$

$$\sigma_{NLO}^{HTL} = 38.66_{-15\%}^{+18\%} \text{ fb}$$

$$m_t = 172.5 \text{ GeV}$$

- renormalization/factorization scale uncertainties @ NLO:

$$\sqrt{s} = 13 \text{ TeV} : \quad \sigma_{tot} = 27.73(7)_{-12.8\%}^{+13.8\%} \text{ fb}$$

$$\sqrt{s} = 14 \text{ TeV} : \quad \sigma_{tot} = 32.81(7)_{-12.5\%}^{+13.5\%} \text{ fb}$$

$$\sqrt{s} = 27 \text{ TeV} : \quad \sigma_{tot} = 127.0(2)_{-10.7\%}^{+11.7\%} \text{ fb}$$

$$\sqrt{s} = 100 \text{ TeV} : \quad \sigma_{tot} = 1140(2)_{-10.0\%}^{+10.7\%} \text{ fb}$$

- m_t scale/scheme uncertainties @ NLO:

$$\sqrt{s} = 13 \text{ TeV} : \quad \sigma_{tot} = 27.73(7)_{-18\%}^{+4\%} \text{ fb}$$

$$\sqrt{s} = 14 \text{ TeV} : \quad \sigma_{tot} = 32.81(7)_{-18\%}^{+4\%} \text{ fb}$$

$$\sqrt{s} = 27 \text{ TeV} : \quad \sigma_{tot} = 127.8(2)_{-18\%}^{+4\%} \text{ fb}$$

$$\sqrt{s} = 100 \text{ TeV} : \quad \sigma_{tot} = 1140(2)_{-18\%}^{+3\%} \text{ fb}$$

- how to combine them? \rightarrow envelope \sim linear sum (rel. err.)

final combined ren./fac. scale and m_t scale/scheme unc. @ NNLO_{FTapprox}:

$$\sqrt{s} = 13 \text{ TeV} : \quad \sigma_{tot} = 31.05^{+6\%}_{-23\%} \text{ fb}$$

$$\sqrt{s} = 14 \text{ TeV} : \quad \sigma_{tot} = 36.69^{+6\%}_{-23\%} \text{ fb}$$

$$\sqrt{s} = 27 \text{ TeV} : \quad \sigma_{tot} = 139.9^{+5\%}_{-22\%} \text{ fb}$$

$$\sqrt{s} = 100 \text{ TeV} : \quad \sigma_{tot} = 1224^{+4\%}_{-21\%} \text{ fb}$$

final combined ren./fac. scale and m_t scale/scheme unc. @ NNLO_{FTapprox}:

$\sqrt{s} = 13 \text{ TeV} :$	$\sigma_{tot} = 31.05^{+6\%}_{-23\%} \text{ fb}$
$\sqrt{s} = 14 \text{ TeV} :$	$\sigma_{tot} = 36.69^{+6\%}_{-23\%} \text{ fb}$

- similar uncertainties for other Higgs masses expected

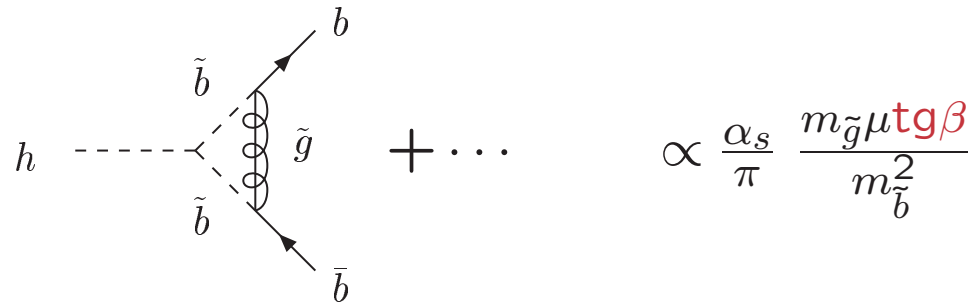
$$\begin{aligned}\sigma(gg \rightarrow HH) &= \sigma_{tt} + \sigma_{tb} + \sigma_{bb} \\ K_{tt} &\sim 1.7 \text{ (incl. } m_t \text{ effects, } \mu = Q/2) \\ K_{tb} &\sim ??? \\ K_{bb} &\sim ???\end{aligned}$$

[grid in M_H ?]

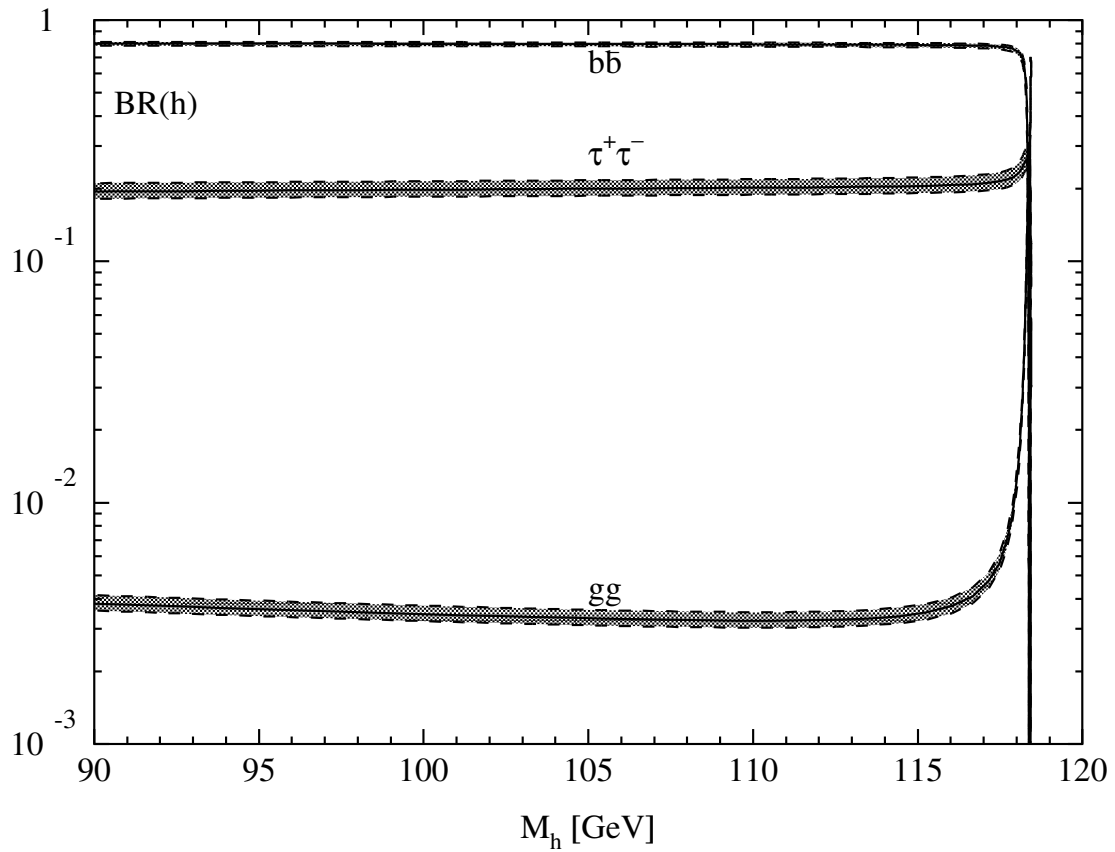
⇒ sizeable uncerts. that affect extraction of BSM/int. contributions

$$\sigma = \sigma_{h^{(*)} \rightarrow H_1 H_2} + \Delta\sigma_{int} + \sigma_{H^{(*)} \rightarrow H_1 H_2} + \sigma_{\square\square} + \sigma_{\Delta\square} + \dots$$

- large SUSY-QCD corrections to $\phi^0 \rightarrow b\bar{b}$



Hall, ...
 Carena, ...
 Nierste, ...
 Guasch, ...
 etc.



Guasch, Häfliger, S.

II Δ_b CORRECTIONS

SUSY-QCD Corrections to $b\bar{b}\phi^0$

$[\Delta \lesssim 1\%]$

$$\begin{aligned} \mathcal{L}_{eff} &= -\lambda_b \bar{b}_R \left[\phi_1^0 + \frac{\Delta_b}{\text{tg}\beta} \phi_2^{0*} \right] b_L + h.c. \quad \text{valid to all orders in } \Delta_b \\ &= -m_b \bar{b} \left[1 + i\gamma_5 \frac{G^0}{v} \right] b - \frac{m_b/v}{1 + \Delta_b} \bar{b} \left[g_b^h \left(1 - \frac{\Delta_b}{\text{tg}\alpha \text{tg}\beta} \right) h \right. \\ &\quad \left. + g_b^H \left(1 + \Delta_b \frac{\text{tg}\alpha}{\text{tg}\beta} \right) H - g_b^A \left(1 - \frac{\Delta_b}{\text{tg}^2\beta} \right) i\gamma_5 A \right] b \end{aligned}$$

$$\Delta_b = \Delta_b^{QCD(1)} + \Delta_b^{elw(1)}$$

$$\Delta_b^{QCD(1)} = \frac{2}{3} \frac{\alpha_s(\mu_R)}{\pi} M_{\tilde{g}} \mu \text{tg}\beta I(m_{\tilde{b}_1}^2, m_{\tilde{b}_2}^2, M_{\tilde{g}}^2)$$

$$\Delta_b^{elw(1)} = \frac{\lambda_t^2(\mu_R)}{(4\pi)^2} \mu A_t \text{tg}\beta I(m_{\tilde{t}_1}^2, m_{\tilde{t}_2}^2, \mu^2)$$

$$I(a, b, c) = -\frac{ab \log \frac{a}{b} + bc \log \frac{b}{c} + ca \log \frac{c}{a}}{(a-b)(b-c)(c-a)}$$

Carena, Garcia, Nierste, Wagner
Guasch, Häfliger, S.

\Rightarrow resummed Yukawa couplings \tilde{g}_b^Φ

small α_{eff} scenario [modified]

$$\text{tg}\beta = 30$$

$$M_{\tilde{Q}} = 800 \text{ GeV}$$

$$M_{\tilde{g}} = 1000 \text{ GeV} \quad \leftarrow$$

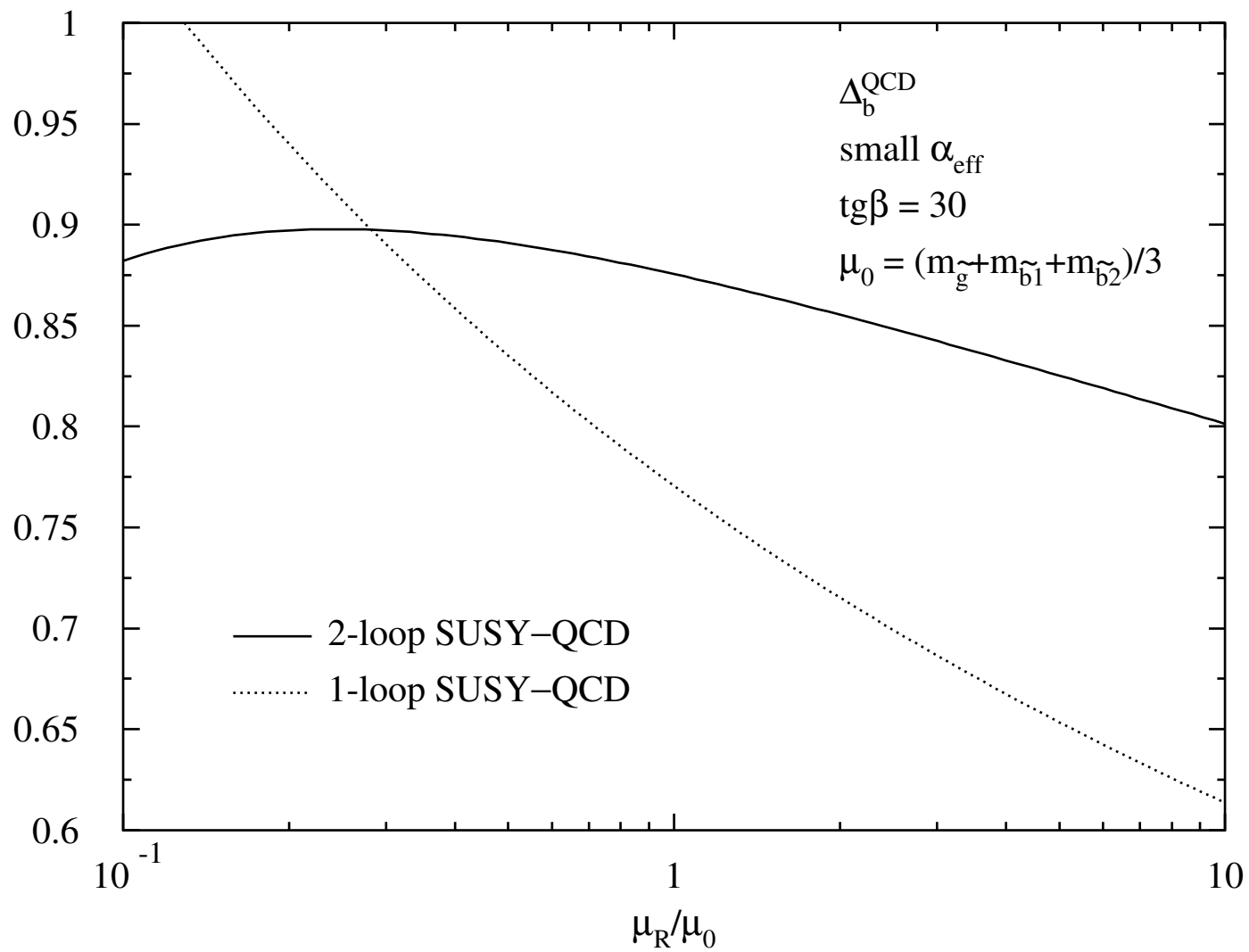
$$M_2 = 500 \text{ GeV}$$

$$A_b = A_t = -1.133 \text{ TeV}$$

$$\mu = 2 \text{ TeV}$$

$$m_{\tilde{t}_1} = 679 \text{ GeV} \quad m_{\tilde{t}_2} = 935 \text{ GeV}$$

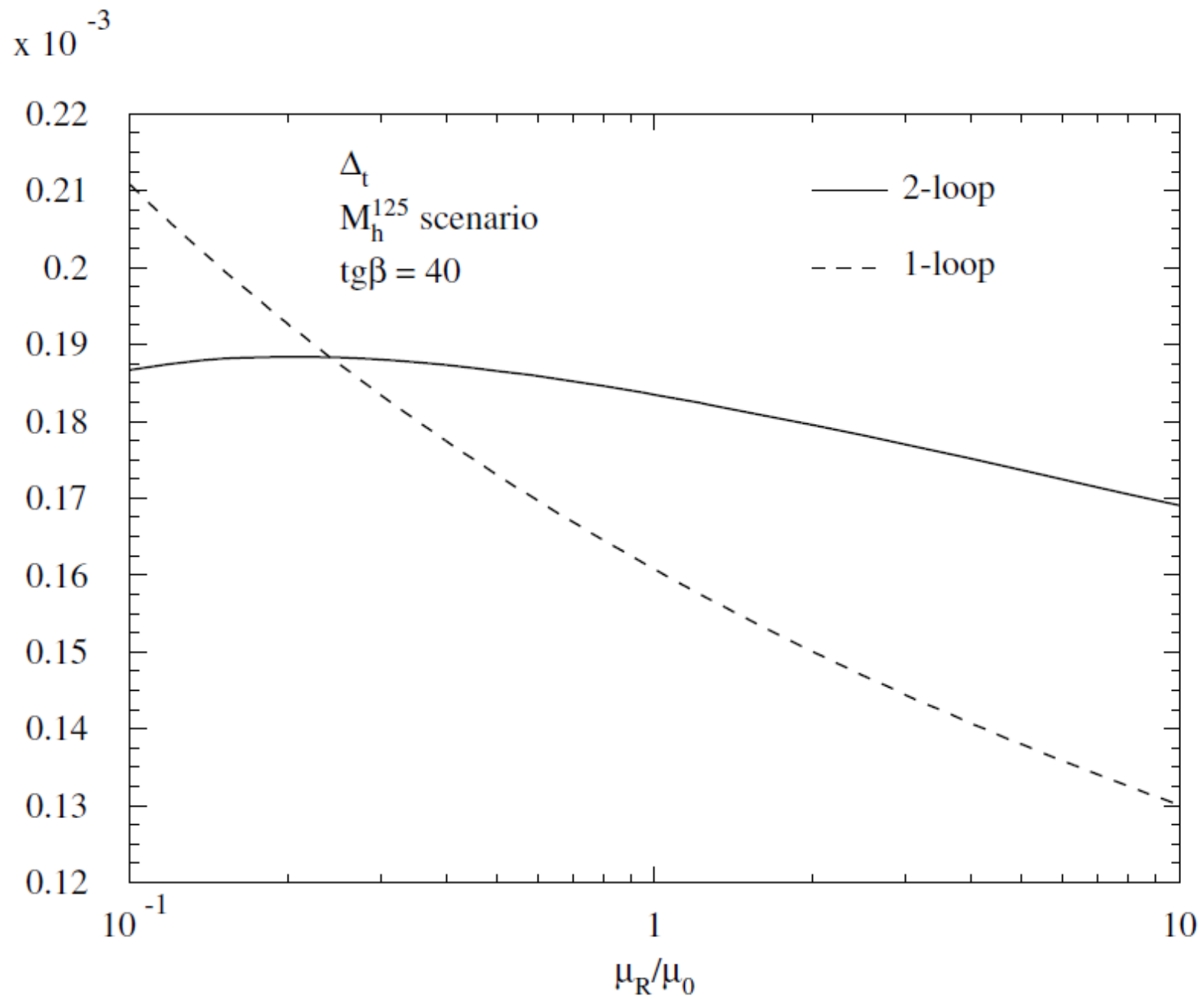
$$m_{\tilde{b}_1} = 601 \text{ GeV} \quad m_{\tilde{b}_2} = 961 \text{ GeV}$$



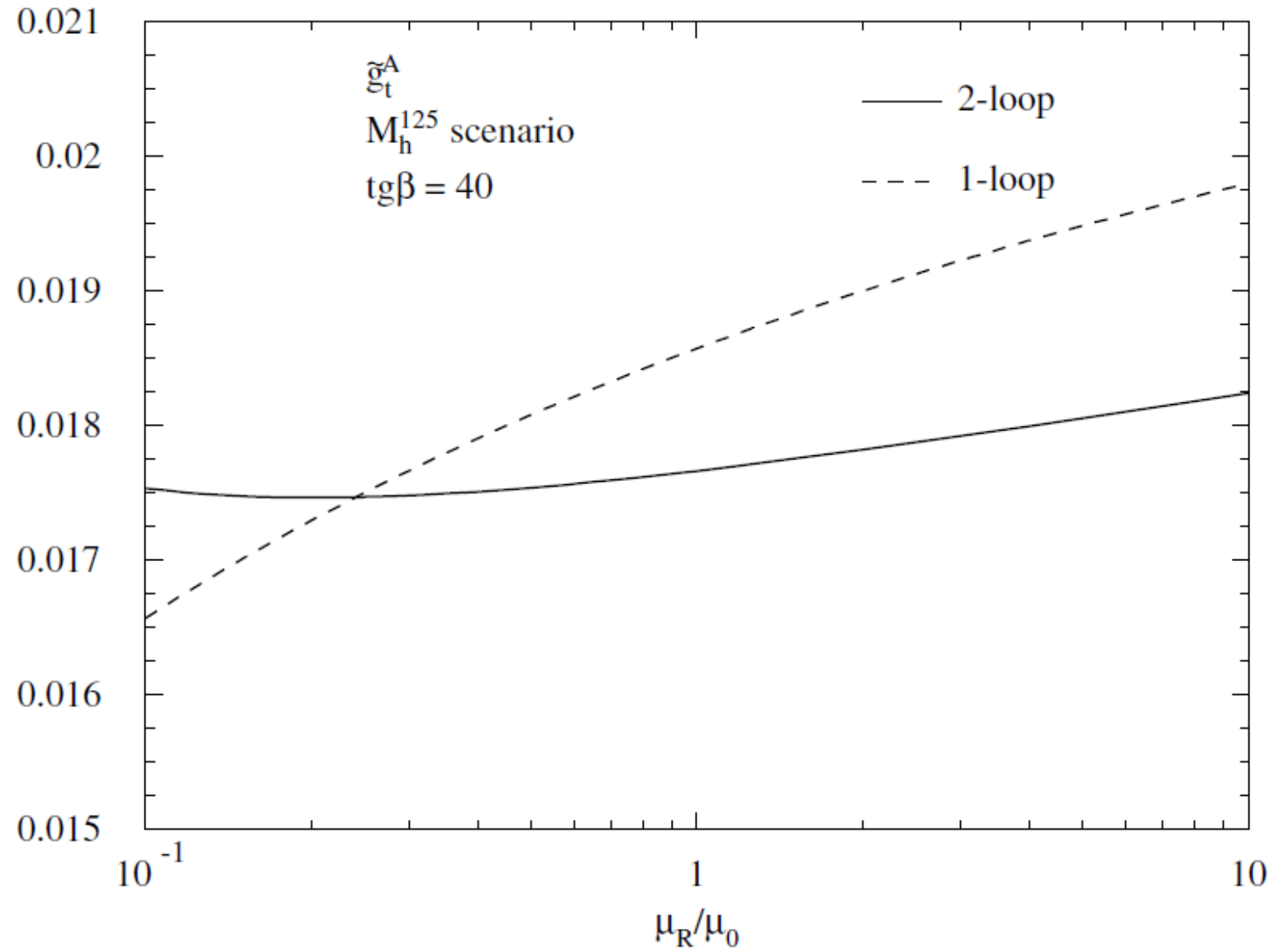
Noth, S.
 (Mihaila, Reisser)

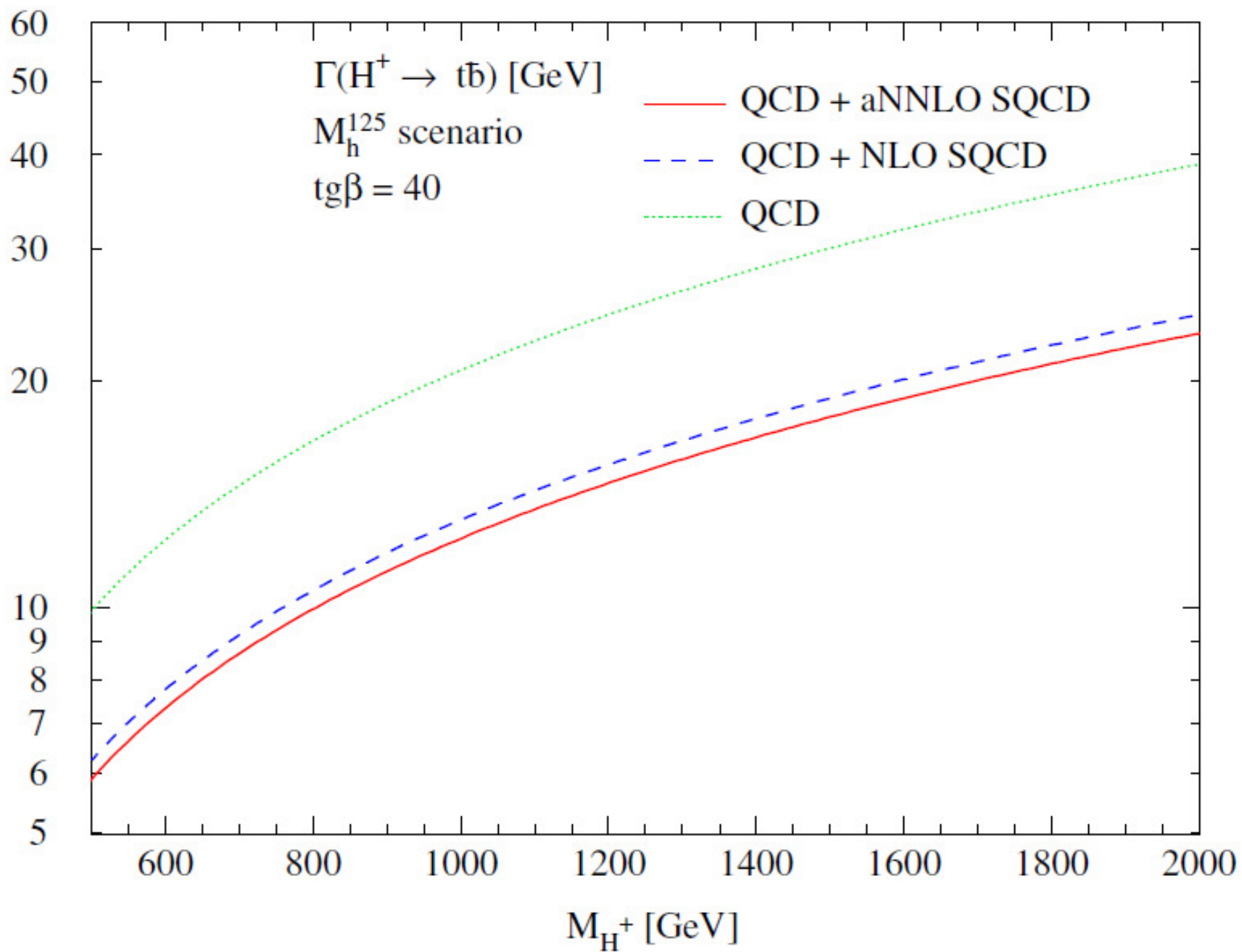
$$\Delta_t = \frac{C_F}{2} \frac{\alpha_s}{\pi} \frac{m_{\tilde{g}} \mu}{\text{tg}\beta} I(m_{\tilde{t}_1}^2, m_{\tilde{t}_2}^2, m_{\tilde{g}}^2)$$

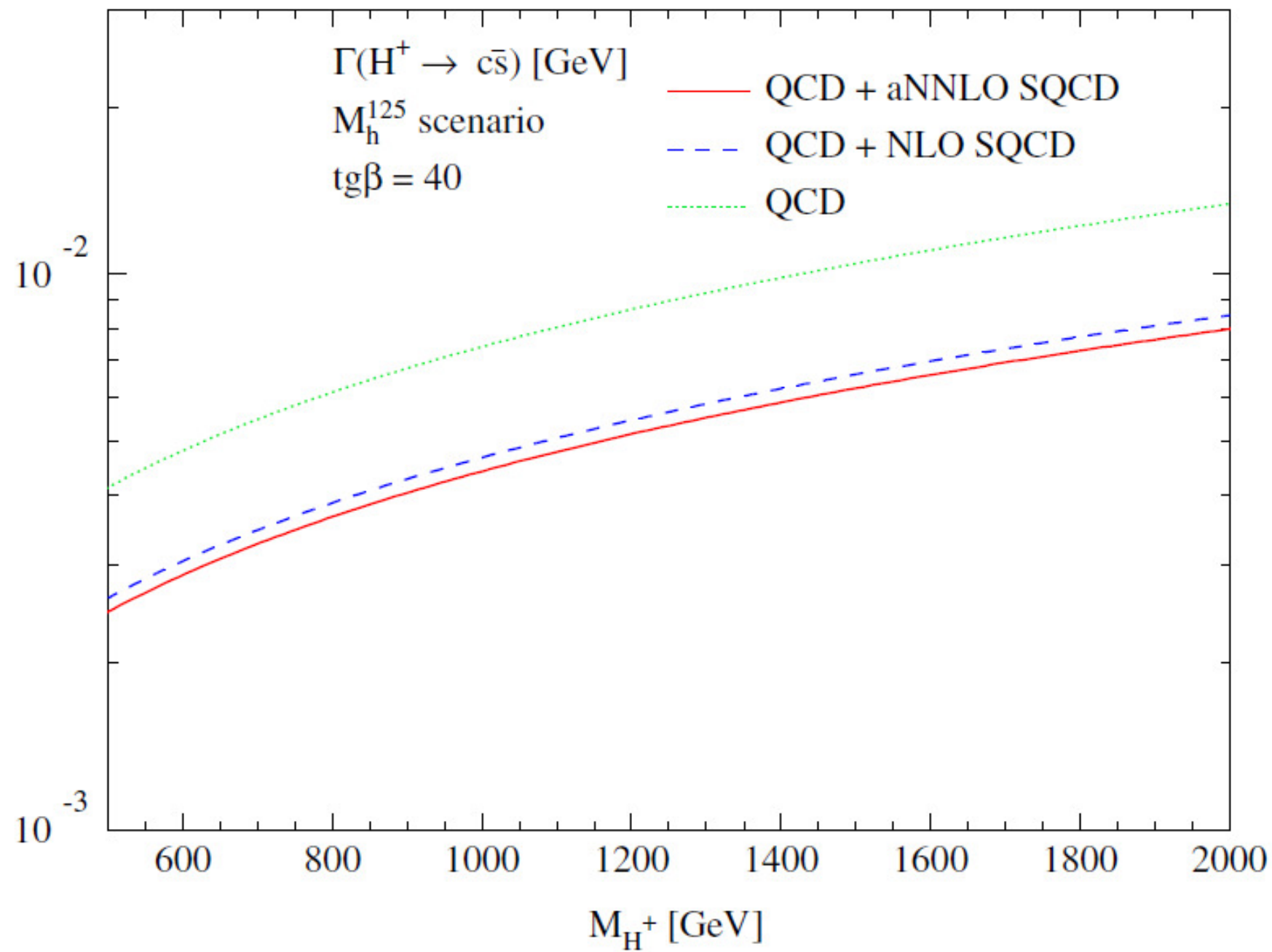
$$\begin{aligned} \mathcal{L}_{eff} &= -\lambda_t \bar{t}_R [\phi_2^0 + \Delta_t \text{tg}\beta \phi_1^{0*}] t_L + h.c. \\ &= -m_t \bar{t} \left[1 - i\gamma_5 \frac{G^0}{v} \right] t - \frac{m_t/v}{1 + \Delta_t} \bar{t} \left[g_t^h (1 - \Delta_t \text{tg}\alpha \text{tg}\beta) h \right. \\ &\quad \left. + g_t^H \left(1 + \Delta_t \frac{\text{tg}\beta}{\text{tg}\alpha} \right) H - g_t^A (1 - \Delta_t \text{tg}^2\beta) i\gamma_5 A \right] t \end{aligned}$$



LO = 0.025







$$\begin{aligned}
\mathcal{O}_1 &= |H|^2 G_{\mu\nu}^a G^{a,\mu\nu}, \\
\mathcal{O}_2 &= |H|^2 \bar{Q}_L H^c t_R + h.c., \\
\mathcal{O}_3 &= \bar{Q}_L H \sigma^{\mu\nu} T^a t_R G_{\mu\nu}^a + h.c.,
\end{aligned}$$

which, for single-Higgs production, can be expanded as:

$$\begin{aligned}
\frac{c_1}{\Lambda^2} \mathcal{O}_1 &\rightarrow \frac{\alpha_s}{\pi v} c_g h G_{\mu\nu}^a G^{a,\mu\nu}, \\
\frac{c_2}{\Lambda^2} \mathcal{O}_2 &\rightarrow \frac{m_t}{v} (1 - c_t) h \bar{t} t, \\
\frac{c_3}{\Lambda^2} \mathcal{O}_3 &\rightarrow c_{tg} \frac{g_S m_t}{2v^3} (v + h) G_{\mu\nu}^a (\bar{t}_L \sigma^{\mu\nu} T^a t_R + h.c.),
\end{aligned}$$

$$\begin{aligned}
c_t(Q^2) &= c_t(\mu_0^2) + \frac{24}{5} \frac{m_t^2(\mu_0^2)}{v^2} c_{tg}(\mu_0^2) \left\{ \left(\frac{\alpha_s(Q^2)}{\alpha_s(\mu_0^2)} \right)^{\frac{5}{6\beta_0}} - 1 \right\}, \\
c_{tg}(Q^2) &= c_{tg}(\mu_0^2) \left(\frac{\alpha_s(Q^2)}{\alpha_s(\mu_0^2)} \right)^{-\frac{7}{6\beta_0}}, \\
c_g(Q^2) &= \frac{\beta_0 + \beta_1 \alpha_s(Q^2)/\pi}{\beta_0 + \beta_1 \alpha_s(\mu_0^2)/\pi} \left\{ c_g(\mu_0^2) - \frac{3\pi}{5 - 6\beta_0} \frac{m_t^2(\mu_0^2)}{v^2} \frac{c_{tg}(\mu_0^2)}{\alpha_s(\mu_0^2)} \left[\left(\frac{\alpha_s(Q^2)}{\alpha_s(\mu_0^2)} \right)^{\frac{5}{6\beta_0} - 1} - 1 \right] \right\},
\end{aligned} \tag{2.4}$$

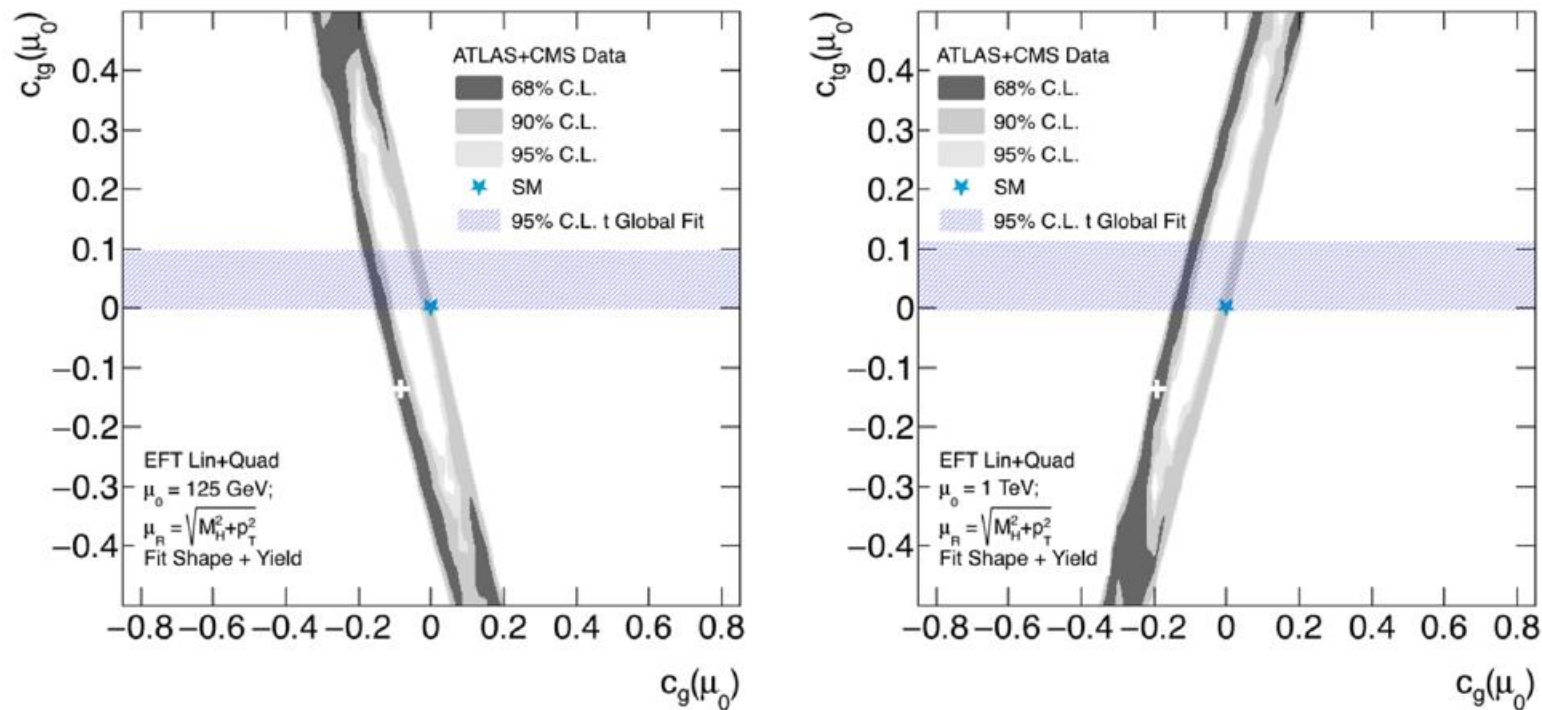


Figure 14. Constraints on the c_g and c_{tg} coefficients at 68% (dark grey), 90% (mid grey) and 95% (light grey) C.L. obtained from the simultaneous fit to ATLAS and CMS data for $\mu_0 = 125$ GeV (left panel) and $\mu_0 = 1$ TeV (right panel). The SM value is indicated by the blue star and the best fit value by the white marker. The shaded horizontal strip indicates the 95% C.L. interval for c_{tg} from the top quark fit of ref. [71] translated to our definition of $c_{tg}(\mu_0)$.