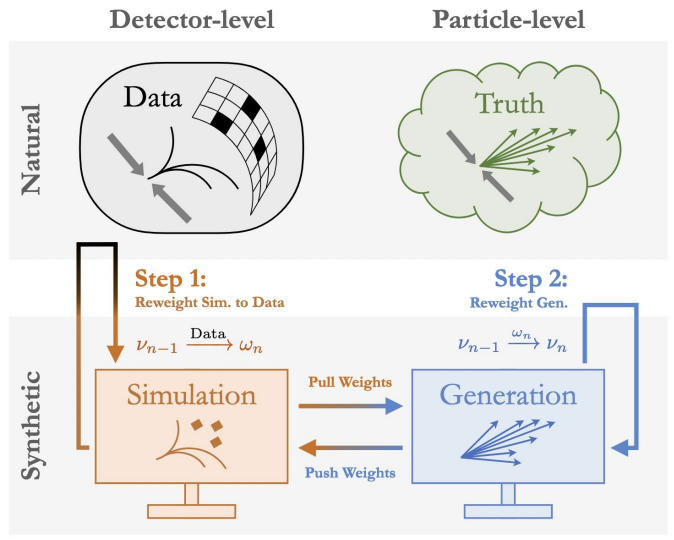




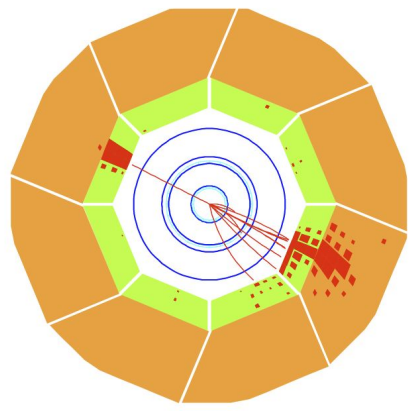
Multi-differential Jet Substructure Measurement in High Q^2 DIS Events with HERA-II Data

Vinicius Mikuni

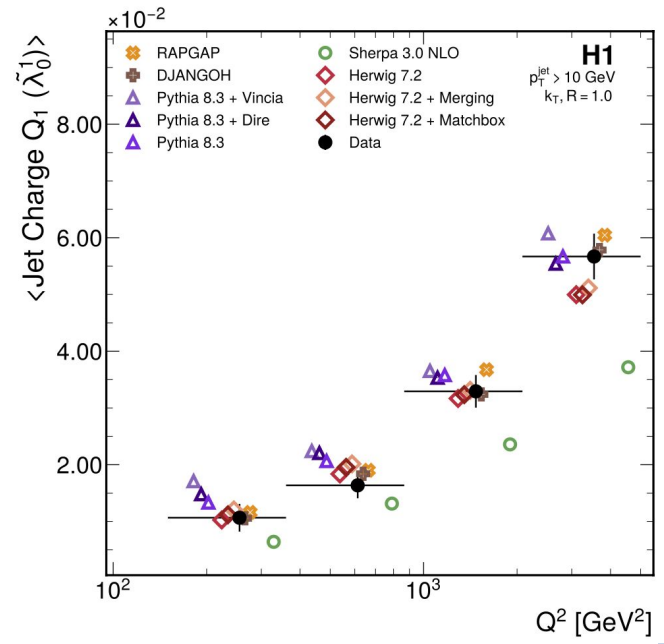
1: Unfolding methodology



2: Definition of measure observables



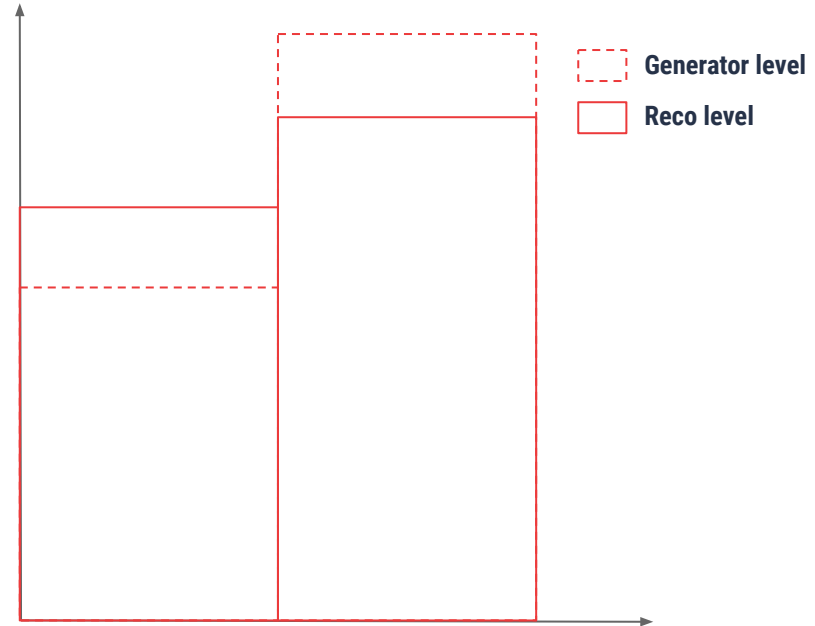
3: Multi-differential cross section results





Unfolding

- We only have access to observables at **reconstruction level**, i.e after detector effects
- When comparing different theories, we want to compare observables before detector interaction (**generator level**):
 - Don't require theorists to have expert detector knowledge to compare their predictions
 - Easier to maintain and incorporate new calibration routines for detector simulation
- What I'm **not** talking about today:
 - [IBU/D'Agostini method](#)
 - [SVD](#)
 - Matrix inversion
 - Other methods for unfolding using histograms





Unfolding

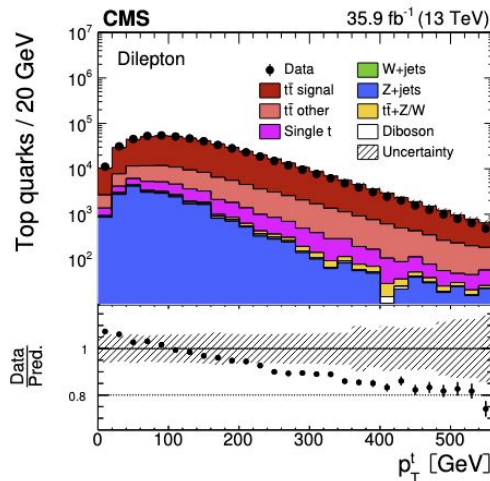
Traditional methods for unfolding are performed using **histograms**

- Well understood statistical properties
- Clear convergence criteria

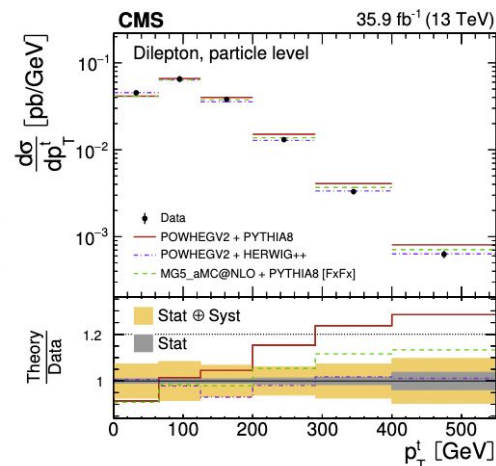
Limitations:

- Histograms need to be defined before unfolding.
 - If a different binning is required, the full unfolding routine needs to be redone
- Often able to address only 1 observable at a time
 - Multi-dimensional histograms are harder to deal with: **curse of dimensionality**

Reco level



Generator level



J. High Energ. Phys. **2019**, 149 (2019).

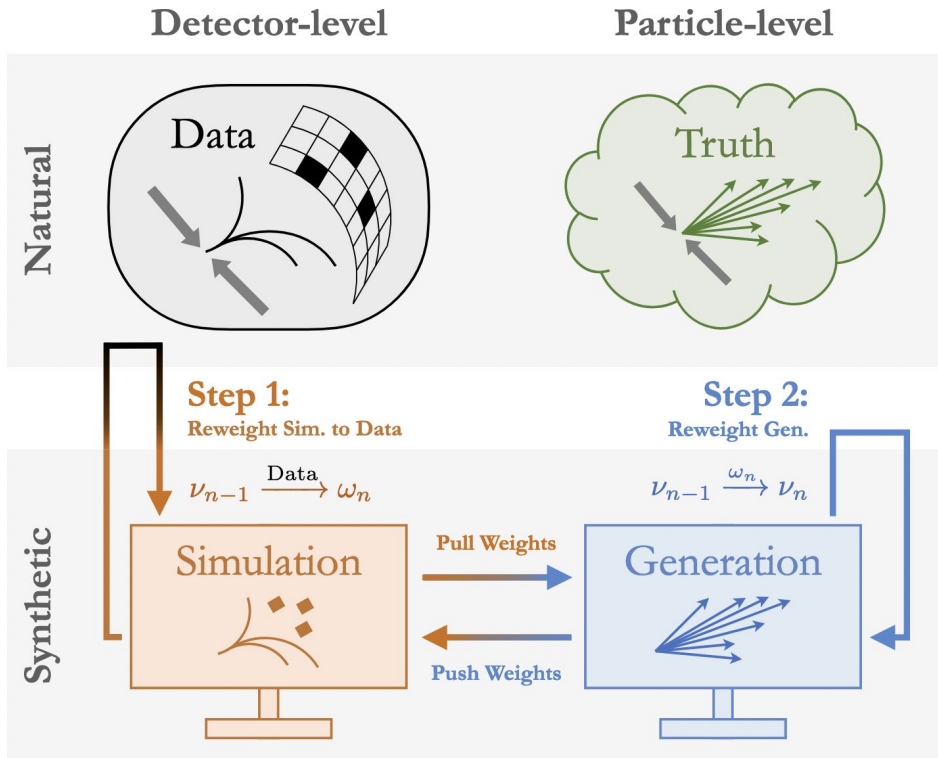


Omnifold*

* Andreassen et al. PRL 124, 182001 (2020)

For unfolding using **invertible networks** see:

- SciPost Phys. 9 (2020) 074 e-Print: [2006.06685](https://arxiv.org/abs/2006.06685)



ML is used to define a method for unfolding that is unbinned and can use multiple distributions at a time
2 step iterative approach

- Simulated events after detector interaction are reweighted to match the data
- Create a “new simulation” by transforming weights to a proper function of the generated events

Machine learning is used to approximate **2** likelihood functions:

- **reco MC to Data** reweighting
- **Previous** and **new Gen** reweighting

* Andreassen et al. PRL 124, 182001 (2020)



Omnifold



Reco level

● Data ○ MC



Generator level

● Data (○) MC



Omnifold



Reco level

● Data ○ MC

Iteration 1



Step 1:

- Train a classifier to separate **data** from **MC** events
- Reweight **reco level MC** with weights:

$W(\text{reco}) =$

$$p_{\text{Data}}(\text{reco}) / p_{\text{MC}}(\text{reco})$$

Generator level

● Data (○) MC



Omnifold



Reco level

● Data ○ MC

Iteration 1



Step 2:

- Pull weights from **step 1** to generator level events
- Train a classifier to separate **initial MC at gen level** from **reweighted MC** events
- Define a **new simulation** with weights that are a **proper function of gen level kinematics**

$$W(\text{gen}) = \frac{p_{\text{weighted}}}{p_{\text{MC}}(\text{gen})}$$



Generator level

● Data (○) MC (○) MC reweighted



Omnifold



Reco level

● Data ○ MC

Iteration 1



Start again from **step 1** using the **new simulation** after **pushing** the weights from **step 2**

- Guaranteed convergence to the maximum likelihood estimate of the generator-level distribution when number of iterations go to infinite
- In practice, less than 10 iterations are enough to achieve convergence

Generator level

● Data (○) MC



Omnifold



Reco level

● Data ○ MC

Iteration N



Start again from **step 1** using the **new simulation** after **pushing** the weights from **step 2**

- **Guaranteed convergence** to the maximum likelihood estimate of the generator-level distribution when number of iterations goes to infinite
- In practice, **less than 10 iterations** are enough to achieve convergence

Generator level

● Data (○) MC

Part 2

Physics case



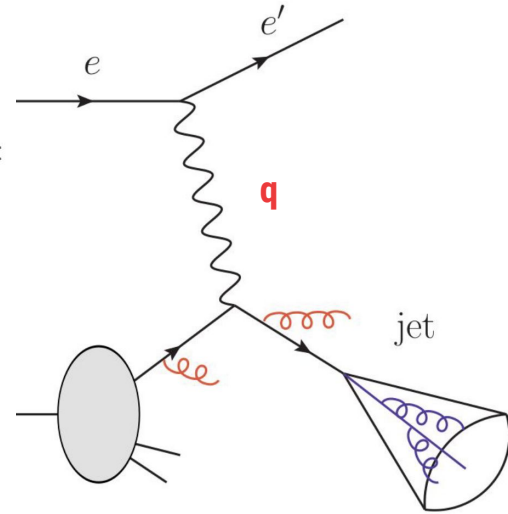
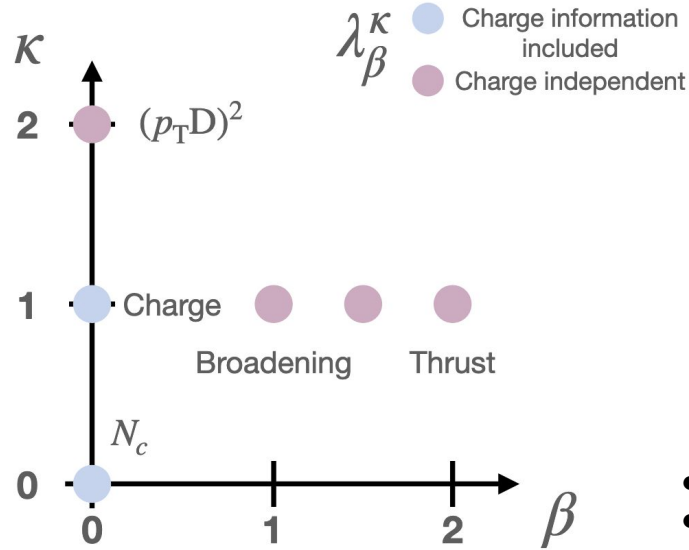
Jet angularities

Use jet observables to study different properties of QCD physics:

- Infrared and collinear (IRC) safe λ_a^1 , $a = [0, 0.5, 1]$ and unsafe $\mathbf{p}_T \mathbf{D}$ angularities
- Charge dependent observables: Q_i and N_c
- Study the evolution of the observables with energy scale $Q^2 = -q^2$

$$\lambda_{\beta}^{\kappa} = \sum_{i \in \text{jet}} z_i^{\kappa} \left(\frac{R_i}{R_0} \right)^{\beta}$$

$$\tilde{\lambda}_0^{\kappa} = Q_{\kappa} = \sum_{i \in \text{jet}} q_i \times z_i^{\kappa}$$



- z_i : longitudinal momentum fraction
- q_i : charge
- R_i : distance from jet axis in (η, ϕ)



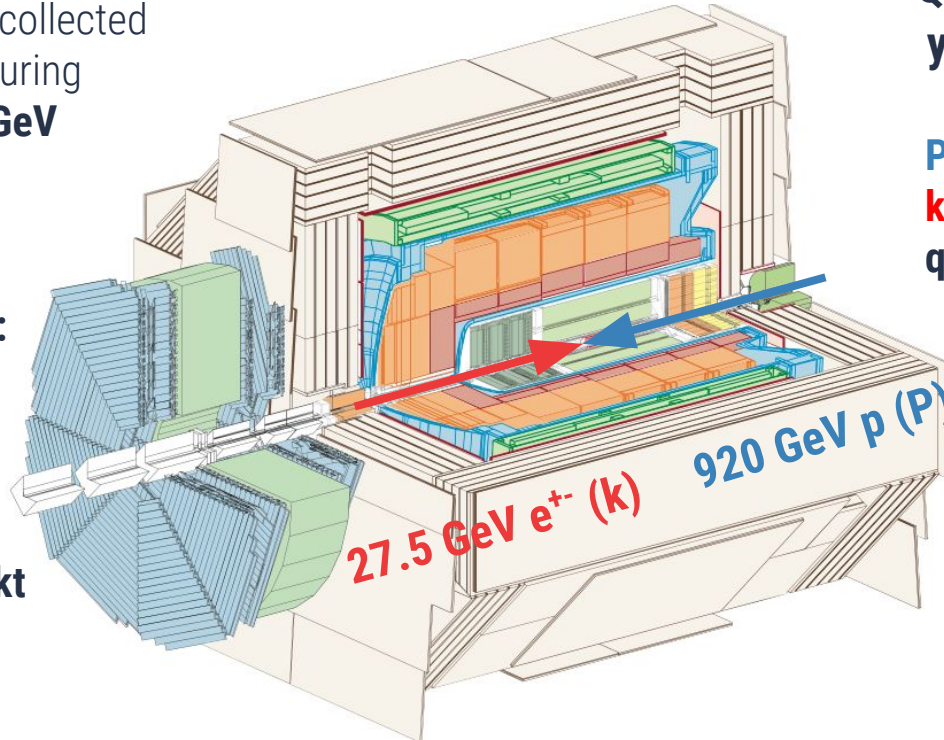
Experimental setup

Using **228 pb⁻¹** of data collected by the **H1 Experiment** during **2006** and **2007** at **318 GeV center-of-mass energy**

Phase space definition:

- $0.2 < y < 0.7$
- $Q^2 > 150 \text{ GeV}^2$
- Jet $p_T > 10 \text{ GeV}$
- $-1 < \eta_{\text{lab}} < 2.5$

Jets are clustered with **kt** algorithm with **R=1.0**



$$Q^2 = -q^2$$
$$y = Pq / pk$$

P: incoming proton 4-vector

k: incoming electron 4-vector

q=k-k': 4-momentum transfer

Reconstructed hadrons using combined detector information: **energy flow algorithm**



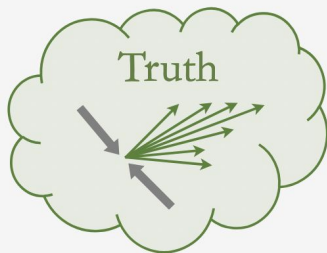
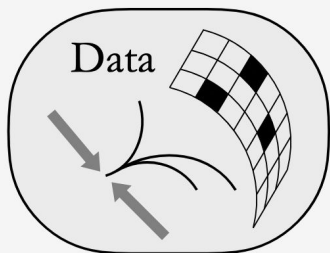
Omnifold*



Detector-level

Particle-level

Natural



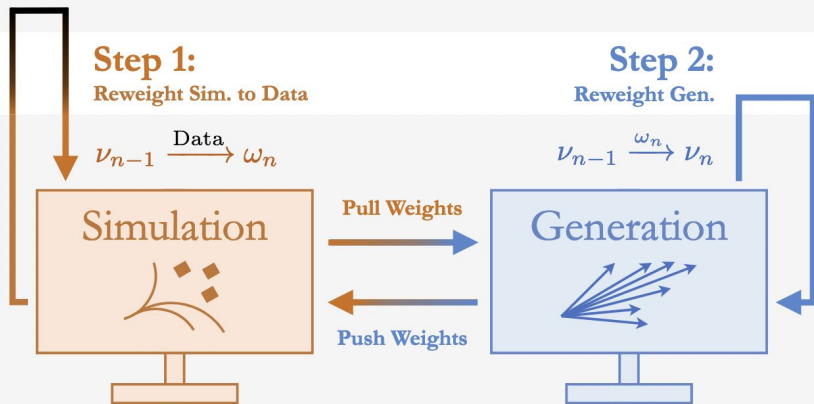
Step 1:
Reweight Sim. to Data

$$\nu_{n-1} \xrightarrow{\text{Data}} \omega_n$$

Step 2:
Reweight Gen.

$$\nu_{n-1} \xrightarrow{\omega_n} \nu_n$$

Synthetic



2 step iterative approach

- Simulated events after detector interaction are reweighted to match the data
- Create a “new simulation” by transforming weights to a proper function of the generated events

Machine learning is used to approximate **2** likelihood functions:

- **reco MC to Data** reweighting
- **Previous and new Gen** reweighting

* Andreassen et al. PRL 124, 182001 (2020)



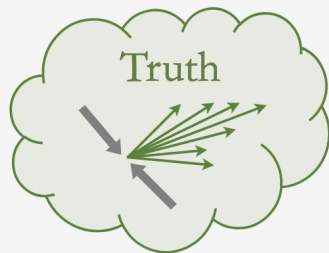
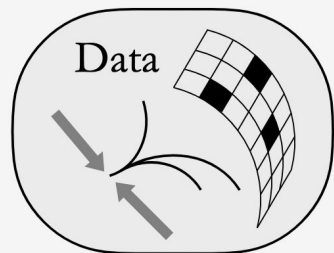
Omnifold



Detector-level

Particle-level

Natural



Step 1:
Reweight G to Data

Reco
Particles
inside jet

Simulation

Pull Weights

Push Weights

Step 2:
Reweight G

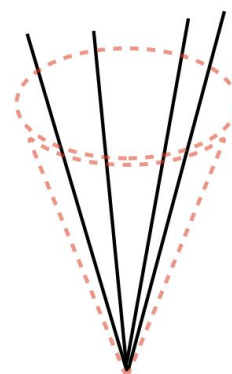
Gen Jet
observables

Generation

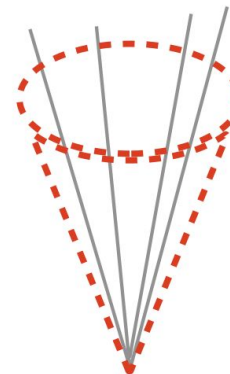
Synthetic

Different input levels for each step

- Step 1 particles are used as inputs
- Step 2 uses the set of observables planned to unfold



Step 1

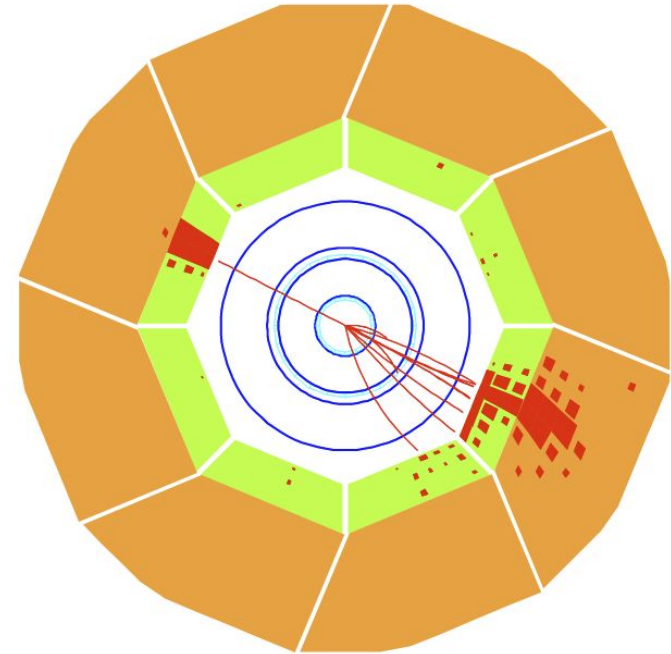
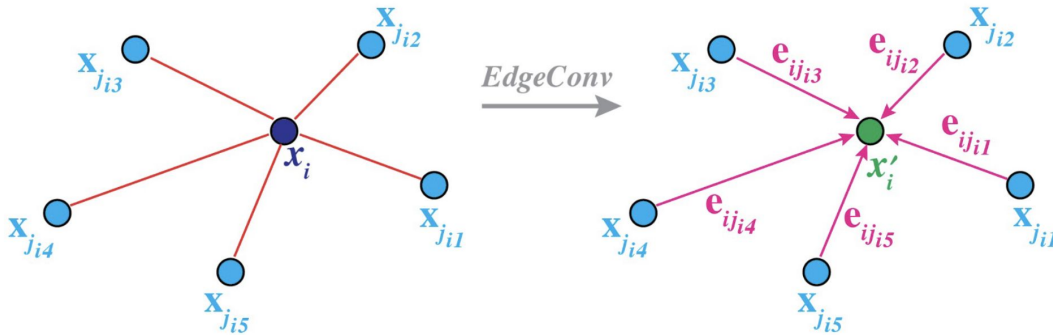


Step 2



Extracting particle information

- Particle information is extracted using a **Point cloud transformer*** model
- Model takes **kinematic properties** of particles and use the distance between particles in η - ϕ to learn the relationship between particles
- Built in symmetries: **permutation invariance**
- Consider up to **30** particles per jet



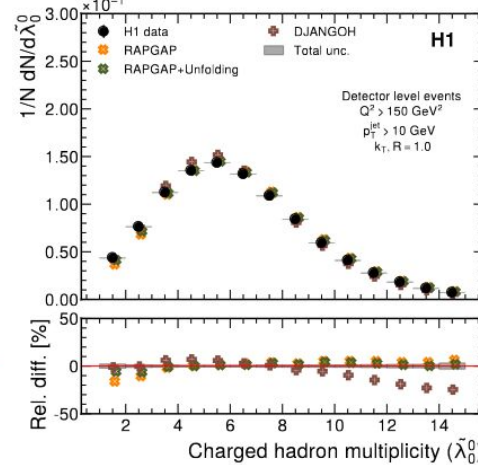
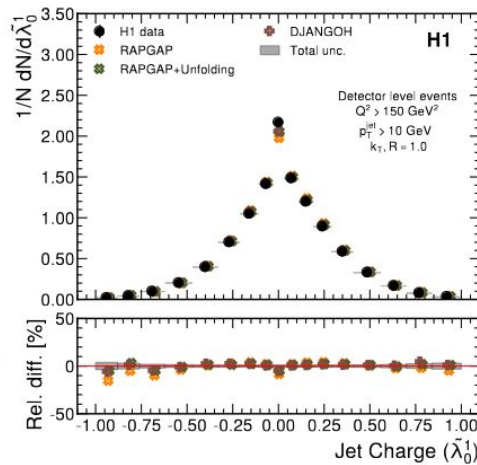
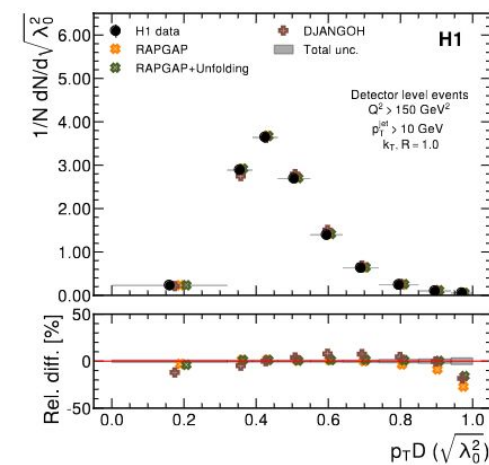
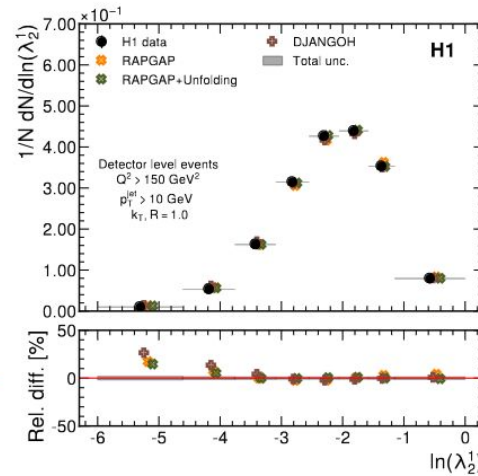
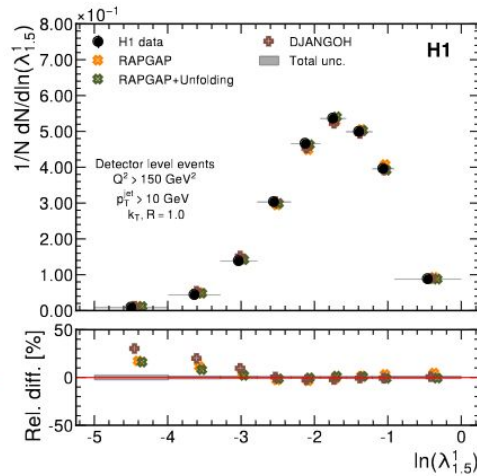
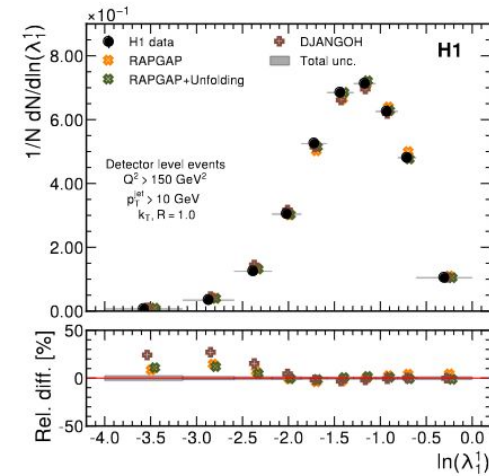


All distributions are **simultaneously** unfolded.



Outputs of the unfolding methodology are **weights** that are applied to the simulation

- **Green markers** represent the unfolded results **at reco level**
- Agreement with data **improves** compared to **initial Rapgap simulation**

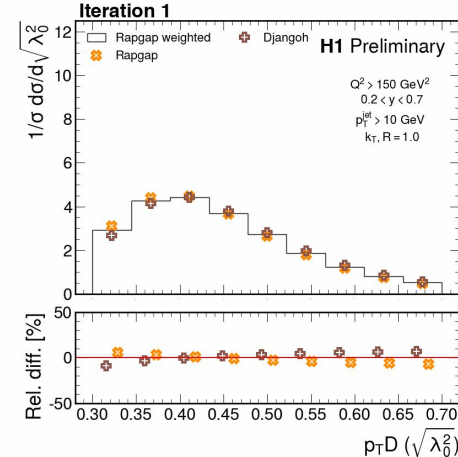
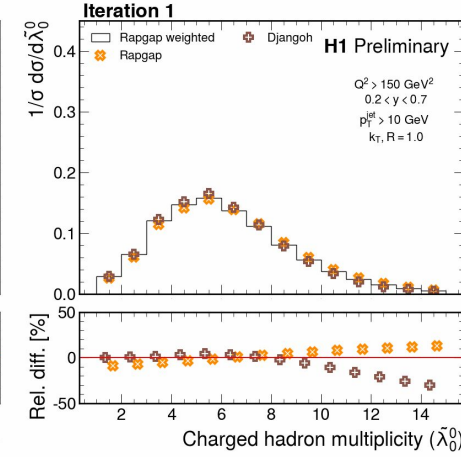
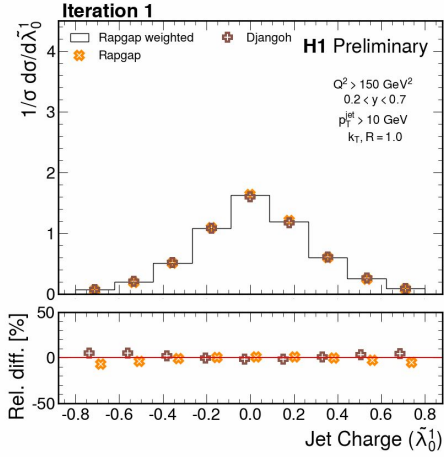
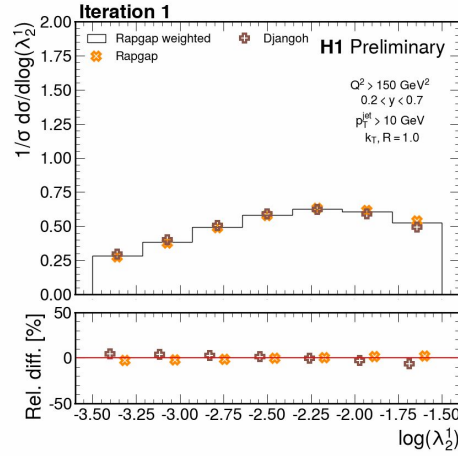
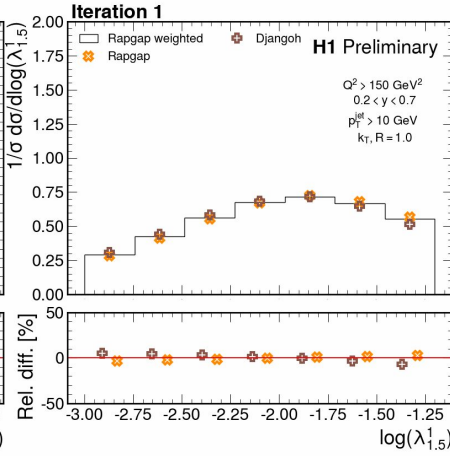
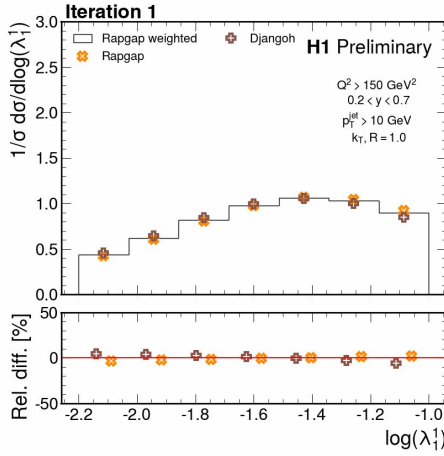


Part 3

Unfolded results



All distributions are unfolded simultaneously without binning and without jet substructure information used at reco level!



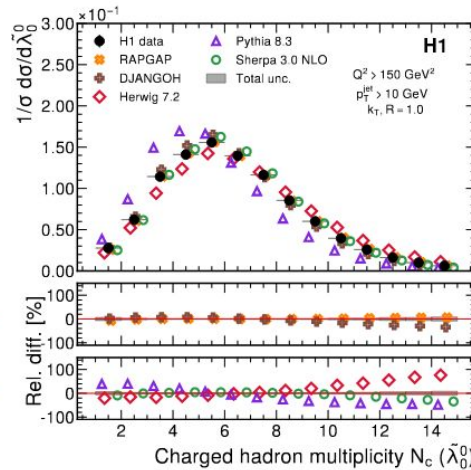
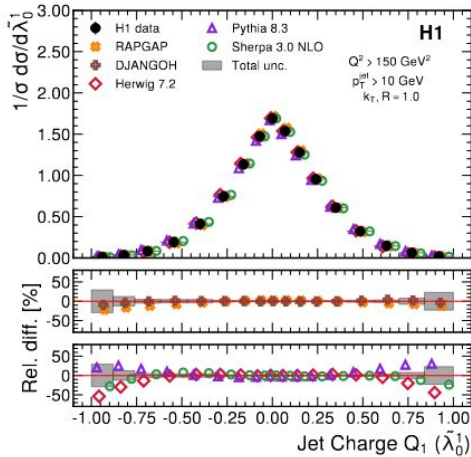
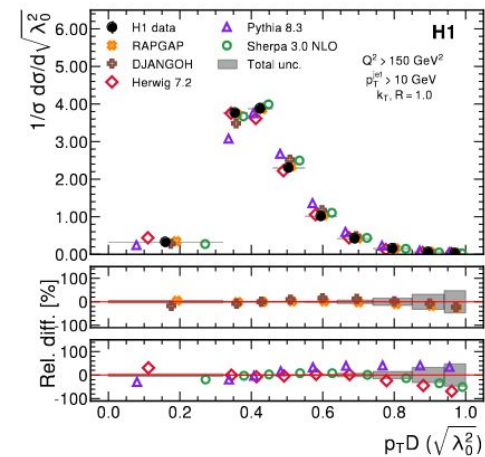
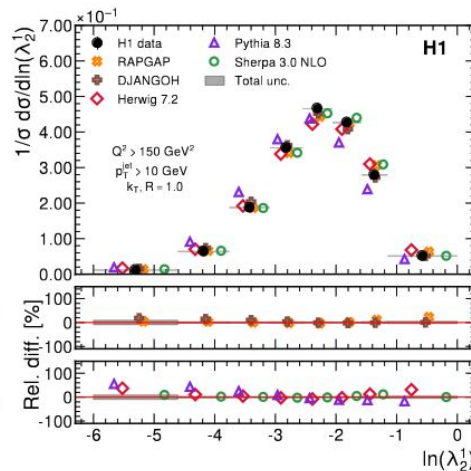
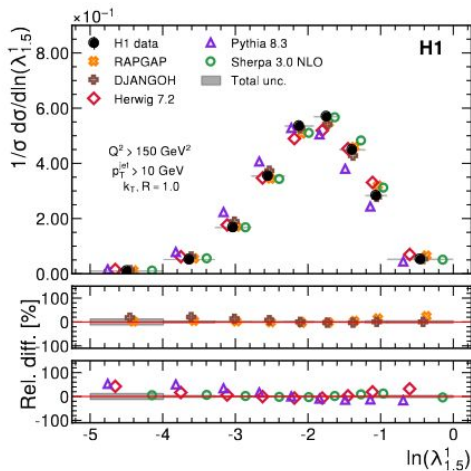
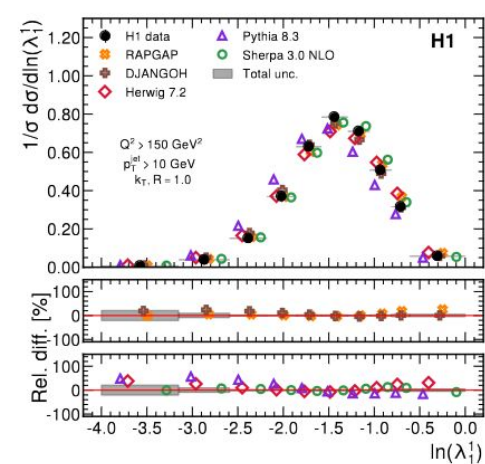
Verify the model **consistency**: start from the **Rapgap** simulation and unfold the response based on the **Djangoh** simulation

Total of **6 iterations** used to derive the main results



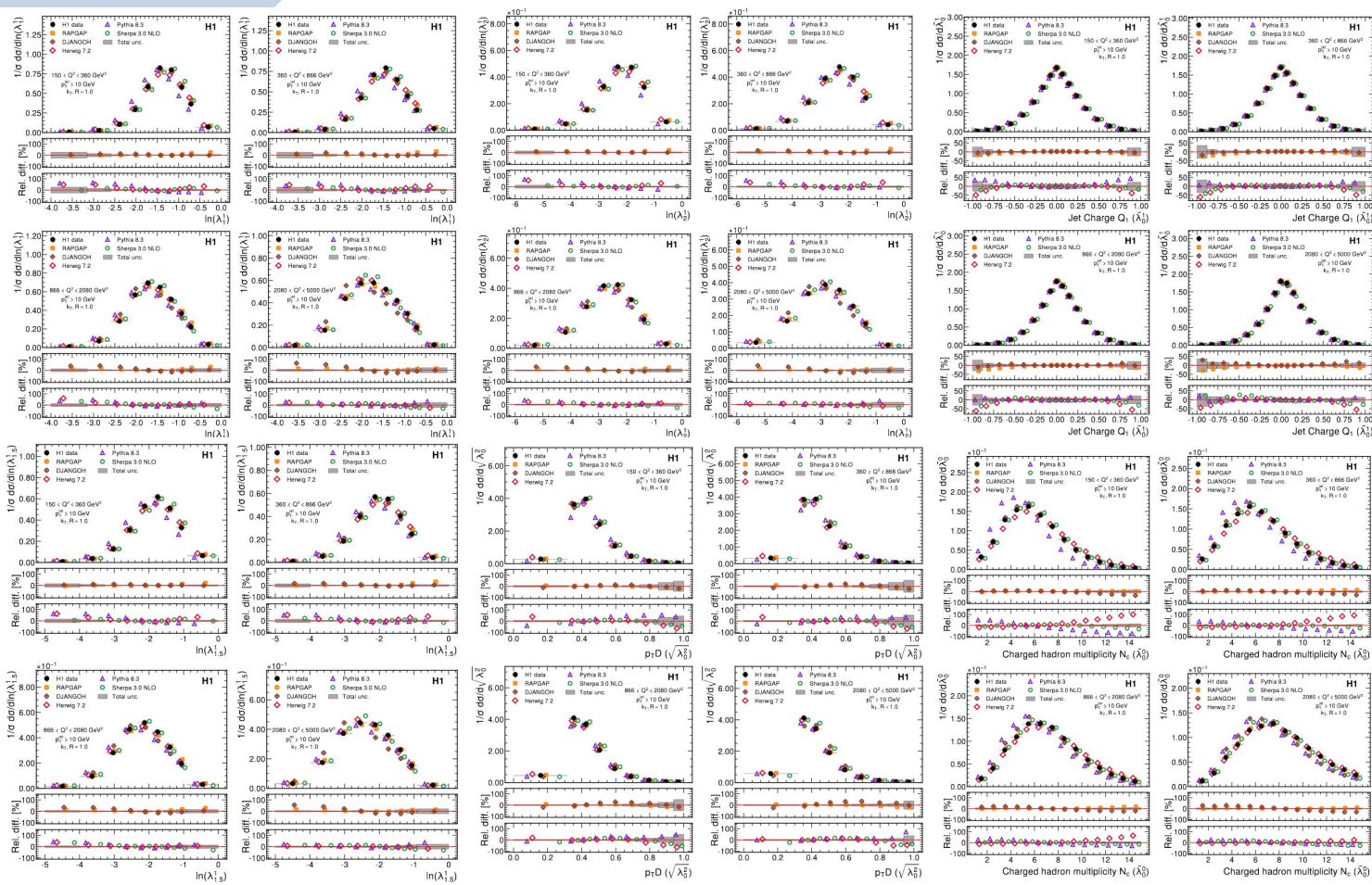
Dedicated DIS generators do a good job **everywhere**, especially **Rapgap**

Herwig, **Pythia**, and (yet unreleased update to) **Sherpa** do a decent job for most distributions





Multi-differential

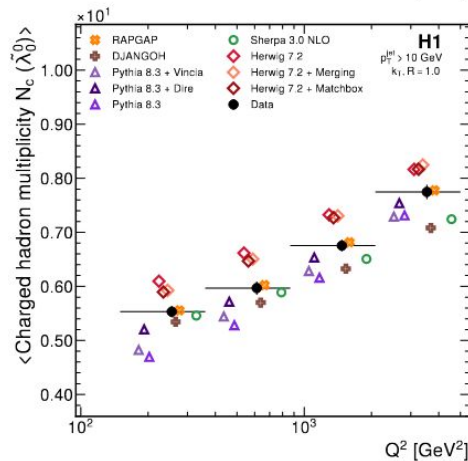
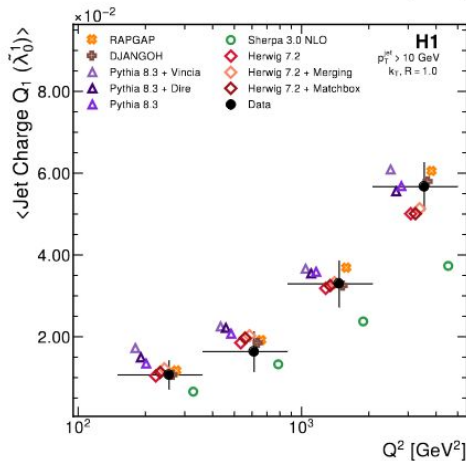
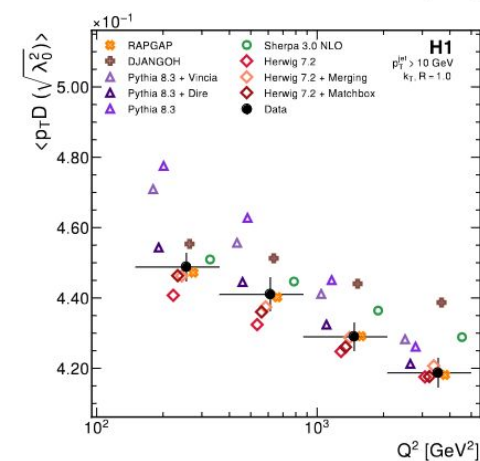
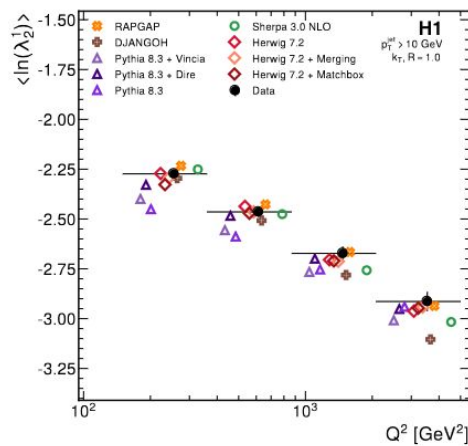
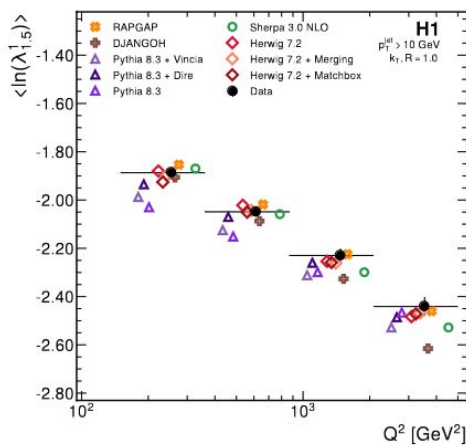
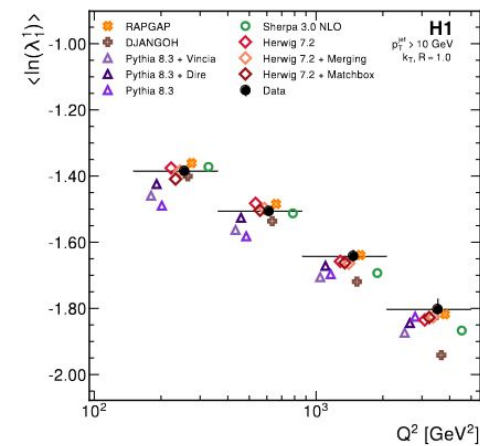


Q^2 distribution is simultaneously unfolded, displaying the energy scale dependence of the observables, resulting in more than 30 unfolded distributions provided



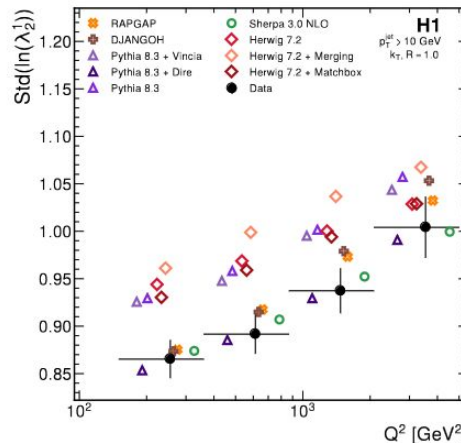
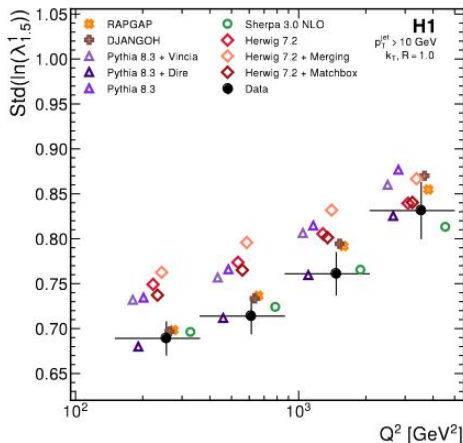
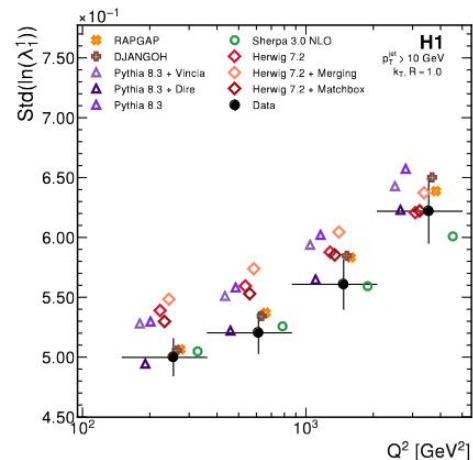
Multi-differential

Mean value of all distributions also unfolded for free

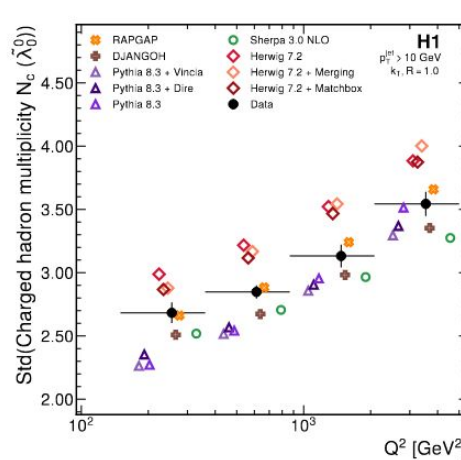
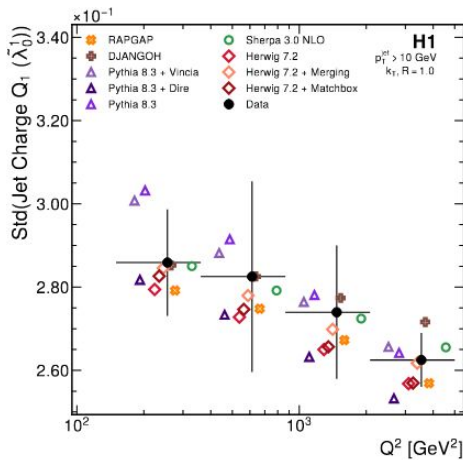
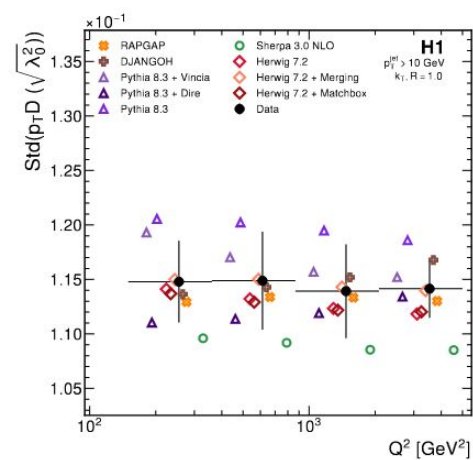


More quark-like behaviour at higher energies: mean jet charge becomes more positive

Agreement between general purpose generators **improve** at higher Q^2



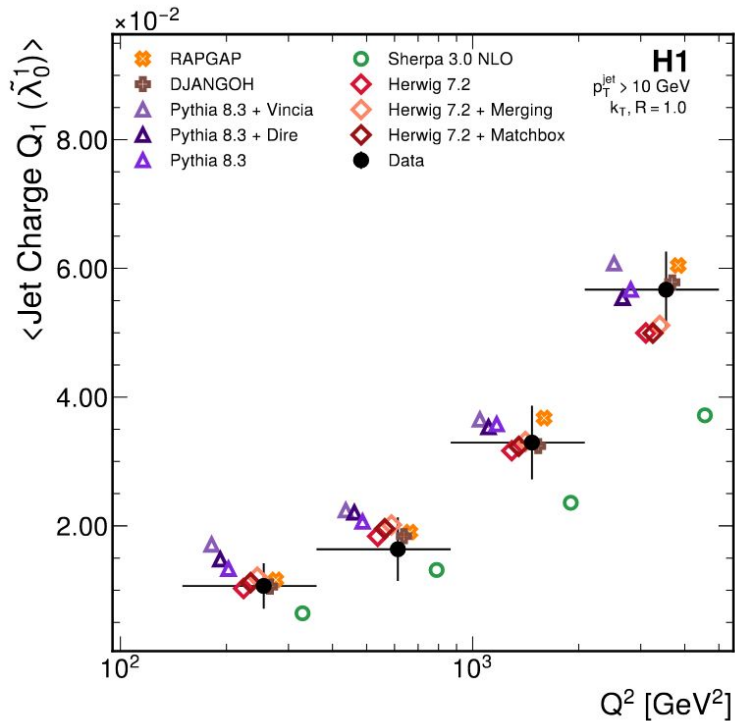
Worse general agreement between data and simulations



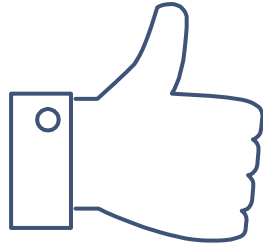
Conclusions



Conclusions and prospects



- Jet observables are an unique laboratory to study **QCD properties**
- **Energy scale** evolution for each jet observable measured in multiple **Q^2 intervals from 150 to 5000 GeV²**
- Detector effects are corrected using the **Omnifold method** with particles as inputs using **graph neural networks**
 - Unbinned and simultaneous unfolding
- Unfolded the means and standard deviations without bin artifacts
- Good agreement for dedicated DIS generators, **worse** agreement for general purpose simulators
- Public results available at: [DESY-23-034](#)



THANKS!

Any questions?

Backup



Systematic uncertainties

Systematic uncertainties currently considered

- **HFS energy scale:** $\pm 1\%$
- **HFS azimuthal angle:** ± 20 mrad
- **Lepton energy:** $\pm 0.5\%$ (mainly affects Q^2)
- **Lepton azimuthal angle:** ± 1 mrad (mainly affects Q^2)
- **Model uncertainty:** differences in unfolded results between Djangoh and Rapgap
- **Non-closure uncertainty:** Differences between the expected and obtained values of the closure test
- **QED uncertainty:** Use the variation of measured quantities when radiation is turned off in the simulation
- **Statistical uncertainty:** Standard deviation of 100 bootstrap samples with replacement



MC Generators

Lund string hadronization model and **CTEQ6L** PDF set

- **Djangoh**: Dipole model from Ariadne
- **Rapgap**: PS from leading log approximation

Pythia 8.3: default NNPDF3.1 PDF

- **Vincia**: p_T ordered antenna and NNPDF3.1 PDF
- **Dire**: dipole model, similar to Ariadne and MMHT14nlo68cl PDF

Herwig 7.2: Cluster hadronization and CT14 PDF set

Sherpa 3.0: Cluster hadronization pQCD at NLO accuracy for the 1 & 2 jet final states and LO for the 3 jet contribution.